

# Joint Video Frame Set Division and Low-Rank Decomposition for Background Subtraction

Jiajun Wen, Yong Xu, *Member, IEEE*, Jinhui Tang, *Member, IEEE*,  
Yinwei Zhan, *Member, IEEE*, Zhihui Lai, and Xiaotang Guo

**Abstract**—The recently proposed robust principle component analysis (RPCA) has been successfully applied in background subtraction. However, low-rank decomposition makes sense on the condition that the foreground pixels (sparsity patterns) are uniformly located at the scene, which is not realistic in real-world applications. To overcome this limitation, we reconstruct the input video frames and aim to make the foreground pixels not only sparse in space but also sparse in time. Therefore, we propose a joint video frame set division and RPCA-based method for background subtraction. In addition, we use the motion as *a priori* knowledge which has not been considered in the current subspace-based methods. The proposed method consists of two phases. In the first phase, we propose a lower bound-based within-class maximum division method to divide the video frame set into several subsets. In this way, the successive frames are assigned to different subsets in which the foregrounds are located at the scene randomly. In the second phase, we augment each subset using the frames with a small quantity of motion. To evaluate the proposed method, the experiments are conducted on real-world and public datasets. The comparisons with the state-of-the-art background subtraction methods validate the superiority of our method.

**Index Terms**—Background subtraction, low-rank decomposition, motion *priori* knowledge, within-class maximum division.

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J. Wen is with the Bio-Computing Research Center, Shenzhen Graduate School, Harbin Institute of Technology, Shenzhen 518055, China, and also with Institute of Textiles and Clothing, Hong Kong Polytechnic University, Hong Kong (e-mail: wenjiajun.hit@gmail.com).

Y. Xu and X. Guo are with the Bio-Computing Research Center, Shenzhen Graduate School, Harbin Institute of Technology, Shenzhen 518055, China (e-mail: yongxu@ymail.com; guoxiaotang.hit@gmail.com).

J. Tang is with the School of Computer Science and Technology, Nanjing University of Science and Technology, Nanjing 210094, China (e-mail: tangjh1981@acm.org).

Y. Zhan is with the Visual Information Processing Research and Development Center, Guangdong University of Technology, Guangzhou 510006, China (e-mail: ywzhan@gdut.edu.cn).

Z. Lai is with the Bio-Computing Research Center, Shenzhen Graduate School, Harbin Institute of Technology, Shenzhen 518055, China, and also with College of Computer Science and Software Engineering, Shenzhen University, Shenzhen 518055, China (e-mail: lai\_zhi\_hui@163.com).

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## I. INTRODUCTION

FOR numerous computer vision tasks, such as indoor surveillance [1], anomaly detection [2], sports video analysis [3], traffic surveillance [4], and so on, background subtraction has been a fundamental step to segment out the motion objects for high-level vision understanding. Usually, the scene suffers from various influence including lighting changes and dynamic backgrounds. Owing to the complex environment and real-time requirement of the surveillance system, many methods [1], [6]–[9] have been proposed to overcome the aforementioned problems. These state-of-the-art methods work well under certain conditions. However, it is not easy to handle all the mentioned problems by using a single method. Generally speaking, background subtraction methods can be classified into three categories: statistic-based methods [5]–[13], classification-based methods [14], [15], and subspace-based methods [1], [16]–[24].

The Gaussian background modeling [5] is a classical statistic-based method and is very popular in the surveillance system. Later researches extended this model to the multi-Gaussian versions [6]–[9] for background subtraction. As these methods are of the parametric-based type whose parameters are hard to learn and adjust under complex environments, [10] and [11] preferred the nonparametric methods for background pixel modeling. However, these methods cannot deal with the continuous changing situations well. Unlike the background subtraction method at the pixel level, [12] and [13] modeled the background at the region level. The region-based method is capable of handling noise, illumination variations, and dynamic environment. Because background subtraction can be viewed as a classification problem, neural network [14] and support vector machines [15] are also exploited for foreground detection. For these methods, a learning procedure is necessary before the detection stage. They show a good adaptation to the learned situations. However, they are not flexible to the new cases that had not been considered in the learning stage. Recent researches on subspace analysis consider that the background lies in a low dimensional subspace, that is, eigenspaces. Such eigenspaces enable the algorithms to resist a variety of contamination. Tsai and Lai [1] assumed that the background and foreground are two independent signals and extracted the foreground by independent component analysis. Cevher *et al.* [16] proposed to use compressive sensing to recover the region of interest. However, the theory requires that the foreground occupies a small portion of the scene. Early in 2000, the classical principal component analysis (PCA) had been used in background modeling [17]. But it is vulnerable when the data is

contaminated by noise. Later, De la Torre and Black [18] extended classical PCA to develop the robust principal component analysis with M-estimation (RPCA-ME), which is more adaptive to noise corruption, alignment errors, and occlusion. Unlike RPCA-ME, the robust principal component analysis (RPCA) model proposed in [19] treats background subtraction as a matrix decomposition problem and is able to recover the low-rank and sparse components of a data matrix even though a quantity of entries of the matrix are contaminated with arbitrary noise intensity.

For a measurement matrix  $M \in \mathbb{R}^{n_1 \times n_2}$  with partial missing entries or being contaminated by noise, there exist many realistic applications that need to recover its original signal and the corresponding noise signal. In other words, we are required to obtain the decomposition  $M = L_0 + S_0$ , where  $L_0$  is a low-rank matrix,  $S_0$  is a sparse matrix, and both components are allowed to have random intensity.

Let  $\sigma_i(M)$  be the  $i$ th singular value of  $M$ , and let  $\|M\|_* := \sum_i \sigma_i(M)$  and  $\|M\|_1 = \sum_{ij} |M_{ij}|$  denote the kernel norm and  $l_1$  norm of matrix  $M$ , respectively. Then under rather weak assumption, RPCA is able to accurately recover low-rank matrix  $L_0$  and sparse matrix  $S_0$  by solving the mathematical model

$$\begin{aligned} & \text{minimize} \|L\|_* + \lambda \|S\|_1 \\ & \text{s. t. } L + S = M. \end{aligned} \quad (1)$$

In the application of background subtraction, the foreground and background in each frame are referred to the sparse and low-rank components of RPCA model. As introduced in [19]–[24], RPCA has given a promising result in background subtraction. The online version of RPCA proposed by Qiu and Vaswani [20] enables the subspace-based background subtraction to be in real time. Mu *et al.* [21] exploited the random projection and SVD to accelerate the calculation efficiency with controllable loss of the performance. Bao *et al.* [22] proposed an inductive RPCA to handle gross corruptions and new data efficiently. Ding *et al.* [23] combined a Bayesian framework with RPCA to broaden the adaptation of the algorithm in a wide range of noise levels. Zhou and Tao [24] proposed a Go Decomposition model and used a bilateral random projection technique to acquire the low-rank and sparse components as well as noise.

It should be noted that the RPCA model makes sense under two assumptions:

- 1) the genuine signal  $L_0$  is of low-rank but not sparse;
- 2) the sparsity patterns should be uniformly distributed in the sparse matrix at random [19].

However, such assumptions may not be fully satisfied in real-world applications. With these reasons, in background subtraction, RPCA still has its own shortcomings. First, it requires the moving objects are uniformly located at random. It fails to detect the objects if they are always located at a limited region of the scene. Second, it does not make use of the motion message. For example, we find out that RPCA is not effective for the rush-hour sequence as shown in Fig. 1(d). Obviously, the rush-hour sequence is full of noise (namely the foreground) that largely decreases the quality of recovering the low-rank

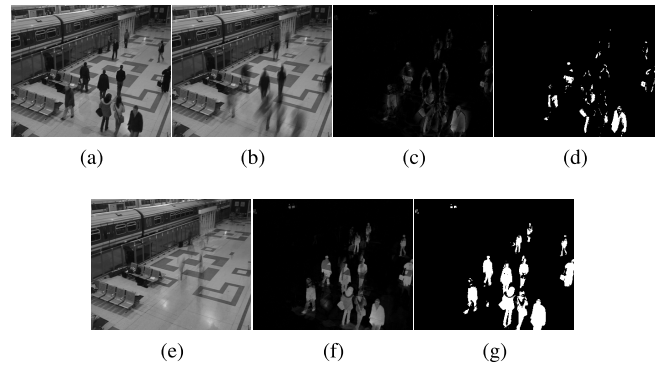


Fig. 1. Results on a rush-hour sequence. (a) Frame from *Pets 2006 s7*. (b) and (c) Low-rank and sparse components of RPCA. (d) Binary image of (c). (e) and (f) Low-rank and sparse components of the proposed method. (g) Binary image of (f).

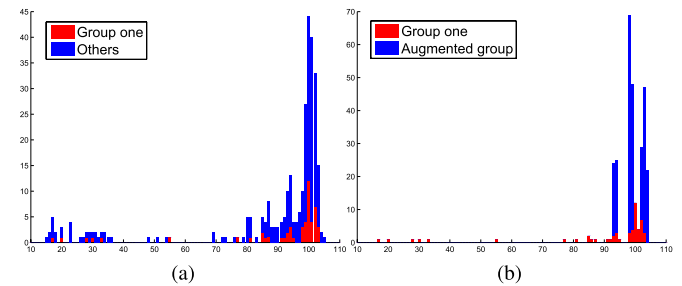


Fig. 2. Statistical distribution of the pixel values of the sequence used in Fig. 1. (a) Statistical distribution of the pixel values. Group one is the statistics of the number of the pixel values from the frame subset obtained by our method. (b) Statistical distribution of the same pixel values by using our augmented method. The augmented group is the statistics of the number of the pixel values from the augmented set obtained by the method in Section V.

and sparse components. Considering the values of a pixel on this sequence, we run all the frames and obtain the statistical distribution of the pixel values [Fig. 2(a)]. The values around 100 give a good estimation of this pixel. However, the values that are far away from 100 come from the moving objects and have side effect on the low-rank decomposition. Our question is: can we make use of the motion message and change the value distribution of the pixel to the one shown in Fig. 2(b)? If it works, it would be much easier and more effective to recover the low-rank and sparse components.

In this paper, unlike RPCA that processes the whole sequence for signal recovery, we take advantage of the motion message and devise a new framework to divide the video frames into several groups. In each group, the statistical distribution of pixel values is supposed to be contaminated by less noise than ever before. The idea of the frame set division and frame set augmentation reduces the motion in each subset and provides more genuine background pixels, which facilitates RPCA to obtain better low-rank and sparse components. First, we estimate the position of the moving objects and ratio of the foreground pixel to all the pixels in each frame by using a simple background subtraction technique. Second, we propose a lower bound-based within-class maximum division (LBWCMD) method to divide the video frame set into several subsets on the basis of the position information. Third, the frames will be ranked in ascending order according to the ratio of the foreground pixel to all the

TABLE I  
VARIABLES OF OUR METHOD

$\Omega$	: Video frame set;
$m$	: Number of divisions of video frame set;
$i$	: A subscript, $i = 1, 2, \dots, m$ ;
$X_i$	: The $i$ -th basic set ( $X_i \subset \Omega$ );
$P_i$	: The $i$ -th division set with motion ( $P_i \subset \Omega$ );
$Q_i$	: The $i$ -th non-motion set ( $Q_i \subset \Omega$ );
$Y_i$	: The $i$ -th augmented set with slight motion ( $Y_i \subset \Omega$ );
$Z_i$	: The $i$ -th group set, $Z_i = X_i \cup Y_i$ .

pixels and the top several frames will be added in each frame subset to construct the groups. Our results on the rush-hour image are shown in Fig. 1(e)–(g). More results are shown in Section VII. To summarize, our contributions are as follows.

- 1) We make use of the motion *priori* knowledge and join the video frame set division and low-rank decomposition for background subtraction. The frame set division is beneficial to the recovery of low-rank and sparse components.
- 2) A new method called LBWCMD is introduced to reconstruct the video frame set to obtain several subsets. The proposed method assigns the successive frames to different subsets as much as possible so that the low-rank decomposition is conducted on each frame subset with less motion. In fact, as shown in Fig. 1(c) and (d), matrix  $M$  constructed by all the frames with highly dense motion is not good for low-rank decomposition.
- 3) We propose a framework to accomplish the background subtraction with frame set division and low-rank decomposition. The framework will be stated in detail in the following sections.

The remainder of the paper is organized as follows. Section II gives an overview of the proposed problem and our solution. Section III shows the estimation of *priori* motion information. Section IV presents the proposed LBWCMD method in detail. Section V illustrates the augmented set construction (ASC) and shows the implementation of the whole framework. Section VI discusses the parameter tuning. The experimental results are described in Section VII. We make a conclusion of this paper in Section VIII.

## II. METHOD OVERVIEW

### A. Problem Statement

The variables used in this problem are shown in Table I. For RPCA-based background subtraction [19], [21], [23], the authors stacked all video frames as column vectors one by one into matrix  $M$ . Then a low-rank decomposition algorithm is performed to recover the low-rank and sparse components [see the flow chart in Fig. 3(a)]. It should be noted that, the highly dense motion appears in a local region has a great impact on the recovery results. It is hard to extract good low-rank and sparse components in such a situation. Therefore, a promising idea is to assign the successive frames to different frame subsets to alleviate such a phenomenon. Our problem is as follows. For a frame set  $\Omega$  with  $|\Omega| = n$ , whether there is a finite division to  $\Omega$ , namely  $\Omega = \bigcup_{i=1,2,\dots,m} X_i$ , when RPCA is applied on  $X_i$  ( $i = 1, 2, \dots, m$ ), the recovery of the low-rank and sparse components is better than that of the low-rank

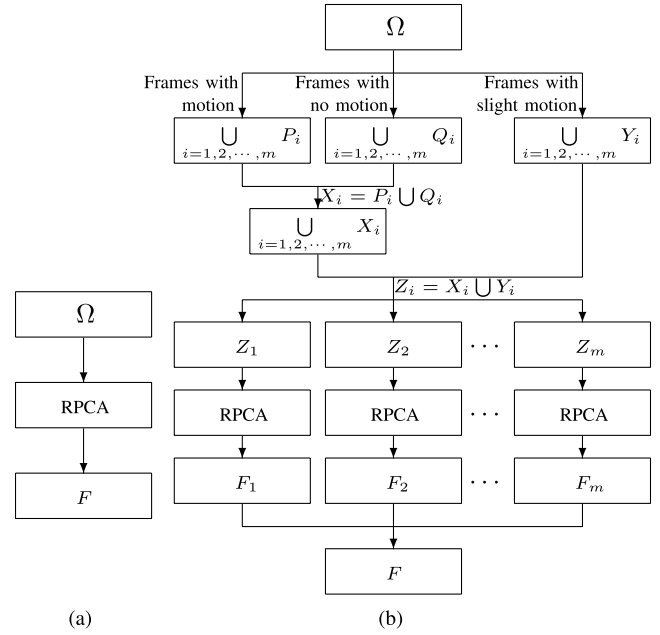


Fig. 3. Flow charts of RPCA and the proposed framework for background subtraction. (a) Flow chart of RPCA for background subtraction. (b) Flow chart of the proposed framework for background subtraction.

and sparse components decomposed from the frame set  $\Omega$ . If it exists, how to obtain such a division?

### B. Proposed Method

The theoretical finding in [19] pointed out that low-rank decomposition makes sense on the condition that the sparsity patterns are uniformly distributed in the sparse matrix at random [19]. However, realistic situations may not satisfy this condition. Therefore, when we divide a video frame set, our division principle is to let the moving objects be uniformly located at random in each subset. This is what the proposed LBWCMD (in Section IV) does to satisfy the aforementioned condition. It should be noted that if successive frames are assigned to the same subset, the sparsity patterns will be restricted in a limited region of the scene which is not good for low-rank decomposition. To this end, successive frames should be assigned to different subsets. Let us study the following division scheme:  $\Omega = \bigcup_{i=1,2,\dots,m} P_i$ ,  $P_i \cap P_j = \emptyset$ ,  $i \neq j$  and each element in  $P_i$  is selected from  $\Omega$  by using LBWCMD method.  $P_i$  can be regarded as division set. However, the scale of  $P_i$  is too small for running RPCA. We propose to make use of the motion *priori* knowledge to devise a new division scheme to make up such a deficiency [Fig. 3(b)]. First, we divide  $\Omega$  into division set  $P_i$  and nonmotion set  $Q_i$ , namely  $\Omega = \bigcup_{i=1,2,\dots,m} P_i \cup \bigcup_{i=1,2,\dots,m} Q_i$  where  $P_i$  consists of the frames with motion and  $Q_i$  consists of the frames with no motion.  $P_i$  and  $Q_i$  can produce a basic set  $X_i = P_i \cup Q_i$ . Then, we extract the frames with slight motion in  $\Omega$  to obtain the augmented set  $Y_i$ , where the elements in  $Y_i$  are not included in  $X_i$ . Finally, the basic set and the augmented set collaborate together to construct group set  $Z_i = X_i \cup Y_i$ . RPCA will be performed on the group sets to run the recovery task. The division set  $P_i$  will be obtained by LBWCMD.



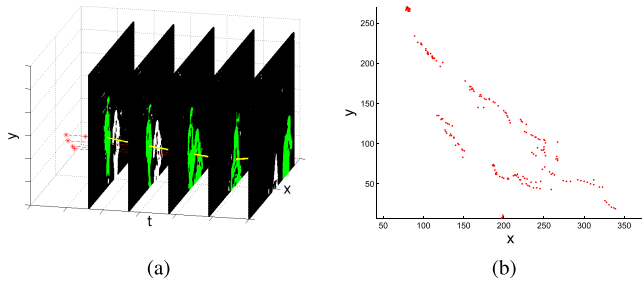


Fig. 4. Centroids of the largest foreground region. (a) Largest foreground region in successive frames. (b) Projections of the centroids on a plane.

Nonmotion set  $Q_i$  and augmented set  $Y_i$  will be obtained using the methods in Section III and V, respectively.

### III. ESTIMATION OF PRIORI MOTION INFORMATION

The motion in the video has a great influence on the quality of low-rank decomposition. For the whole sequence, if the moving objects appear in a local region of the scene, then according to our analysis as described in Section II-B, the low-rank decomposition results will not be good. Thus, we use a new designed strategy to scatter the successive frames to different subsets. Before the division tasks, we need to evaluate the motion *priori* knowledge in advance. In this section, we estimate and use the ratio of the moving area and the centroids of the objects. To this end, a simple background subtraction technique [5] is used to extract the moving information.

We take the centroid of the largest foreground block in each frame as a division criterion. The reasons are as follows.

- 1) The largest block in the foreground reflects the major movement in a frame. Fig. 4(b) shows the projection of all the centroids of the largest foregrounds in a plane. It gives a clear picture of the motion distribution.
- 2) The utilization of the centroid of the largest foreground block can accelerate data processing.
- 3) Adjacent centroids can reveal the continuous movement of the object along the time axis, as the positions of an object in successive frames are normally the nearest.

By performing the simple background subtraction method [5], we can obtain a coarse motion estimation. Fig. 4(a) shows that the foreground images are in alignment along the time axis. Both the green area and white area are the foregrounds in each frame, whereas the green part is the largest foreground block. The centroid of the largest foreground block can be viewed as a representation of the foreground. It roughly reflects the motion distribution of a video sequence [Fig. 4(b)]. We summarize the procedure of the motion *priori* knowledge estimation as follows.

For  $n$  video frames  $I^{(k)} \in \mathbb{N}^{h \times w}$ , ( $k = 1, 2, \dots, n$ ), let  $B^{(k)}$ ,  $F^{(k)}$  be the corresponding background and foreground. Let  $\alpha \in (0, 1)$  be a weight coefficient.

First, we obtain the foreground of the  $k$ th frame using

$$F^{(k)} = |I^{(k)} - B^{(k-1)}| \quad (2)$$

and thresh the foreground into binary image FG using

$$FG(x, y) = \begin{cases} 255 & F^{(k)}(x, y) > T \\ 0 & F^{(k)}(x, y) \leq T \end{cases} \quad (3)$$

where  $T$  is a predefined threshold. Update the corresponding background using

$$B^{(k)} = \alpha I^{(k)} + (1 - \alpha) B^{(k-1)}. \quad (4)$$

Then we find the largest foreground block through optimizing

$$S = \arg \max_{FA_j} \text{Area}(FA_j) \quad (5)$$

where  $FA_j$  is the  $j$ th foreground block of FG and  $\text{Area}(x)$  is the total number of nonzero pixels in  $x$ . Calculate the center of  $S$  to obtain

$$c = \left( \frac{\sum x S(p, q)}{\sum S(p, q)}, \frac{\sum y S(p, q)}{\sum S(p, q)} \right) \quad (6)$$

and update the centroid set, namely

$$\Phi^{(k)} = \Phi^{(k-1)} \cup \{c\}. \quad (7)$$

Finally, we obtain the centroid set  $\Phi^*$  as soon as we go through  $n$  video frames.

The basic set  $X_i (i = 1, 2, \dots, m)$  consists of the division set  $P_i$  and nonmotion set  $Q_i$ . The nonmotion set  $Q_i$  is easily obtained and it is used for reducing the ratio of contamination in the frame set. The reason for using the division set  $P_i$  is to scatter the successive frames as much as possible. We will discuss how to obtain  $P_i$  in the next section.

## IV. LBWCMD METHOD

### A. Model of Frame Set Division

To alleviate the influence of the motion on low-rank decomposition, we consider to reconstruct the frame set  $\Omega$  to obtain the group sets  $Z_i (i = 1, 2, \dots, m)$  where  $\Omega = \bigcup_{i=1,2,\dots,m} Z_i$ . As mentioned in Section II-B, the division set  $P_i$  constitutes an important part of the group set  $Z_i$ . As the centroid set  $\Phi$  of the video has been obtained, we divide the frames to acquire the division set  $P_i$  according to the locations of the centroids. To this end, the following two facts should be considered.

- 1) The successive frames with motion should be assigned to different subsets as much as possible.
- 2) The spatial distribution of the centroid set of each frame subset should be consistent with the spatial distribution of the centroid set of  $\Omega$ .

The former tries to apportion the recovery work to each subset, and the latter guarantees the centroids in each subset come from the whole scene, not a local region of the scene. To start with, we list the variables used in the following models in Table II.

To model the first fact, we use a strategy  $U$  to divide the frame set  $\Omega$  and we have  $\Omega = \bigcup_{k=1,2,\dots,m} \Psi_k$ ,  $\Psi_k \cap \Psi_l = \emptyset (k \neq l)$ . Then, a probability optimization is used to describe the problem [see the mathematical model (8)]. In other words,  $U_{\text{opt}}$  should maximize the combinational probability of  $A_{\text{ip}}^U$  and  $A_{\text{jq}}^U$ , namely the probability of successive frames being assigned to different subsets. For our problem, we constrain  $\delta$  to a small value so as to control the distribution manner of the successive frames. If we set  $\delta = 1$ , it means the

TABLE II  
VARIABLES OF THE PROPOSED MODELS

$U$	: A division which divides the frames into different subsets;
$\Psi_k$	: The $k$ -th subset of $\Omega$ ;
$A_{i_k}^U$	: The event that frame $I_i$ is assigned to $\Psi_k$ with division $U$ ;
$\Gamma$	: A centroid set of $\Omega$ ;
$n$	: The number of the centroids of $\Gamma$ ;
$x_i$	: A centroid of the $i$ -th frame of $\Omega$ ;
$\Upsilon_k$	: The $k$ -th centroid set of $\Psi_k$ ;
$y_{k_j}$	: The $j$ -th centroid of $\Upsilon_k$ ;
$H_\Gamma$	: The convex set of $\Gamma$ ;
$H_{\Upsilon_k}^U$	: The convex set of $\Upsilon_k$ with division $U$ ;
$r$	: a radius;
$N_{(x,r)}^U$	: The number of the centroids in a ball with centroid $x$ and radius $r$ .

successive frames will be assigned to different subsets as much as possible

$$U_{\text{opt}} = \arg \max_U \sum_{\substack{i \neq j \\ i, j \in \{1, 2, \dots, n\}}} P(A_{ip}^U, A_{jq}^U, p \neq q \mid |i - j| \leq \delta). \quad (8)$$

To model the second fact, not only the local similarity but also the global similarity between the spatial distributions of the centroid set  $\Gamma$  and  $\Upsilon_k$  needs to be considered. Therefore, we put forward that the following two goals should be achieved as much as possible.

- 1) The convex hull  $H_{\Upsilon_k}^U$  of the centroid set  $\Upsilon_k$  should occupy almost the same space as the convex hull  $H_\Gamma$  of the centroid set  $\Gamma$ .
- 2) The density of the centroid set  $\Upsilon_k$  should be almost the same as the density of the centroid set  $\Gamma$ .

For the first goal, our model is as follows. Let  $\Gamma = \{x_i, i = 1, 2, \dots, n\}$  be the centroid set of  $\Omega$ . With division  $U$ , the centroid set  $\Gamma$  is divided into  $m$  subsets  $\Upsilon_k = \{y_{kj}, j = 1, 2, \dots, n_k\} (k = 1, 2, \dots, m)$ , that is,  $\Gamma = \bigcup_{k=1, 2, \dots, m} \Upsilon_k, \Upsilon_k \cap \Upsilon_t = \emptyset (k \neq t), \sum_{k=1}^m n_k = n$ . The convex hulls of  $\Gamma$  and its subset  $\Upsilon_k$  are

$$H_\Gamma = \left\{ \sum_{i=1}^n \eta_i x_i \mid x_i \in \Gamma, \sum_{i=1}^n \eta_i = 1, \eta_i \in [0, 1] \right\}, \quad (9)$$

and

$$H_{\Upsilon_k}^U = \left\{ \sum_{j=1}^{n_k} \zeta_j y_{kj} \mid y_{kj} \in \Upsilon_k, \sum_{j=1}^{n_k} \zeta_j = 1, \zeta_j \in [0, 1] \right\}. \quad (10)$$

Therefore, the first goal proposed for the second fact seeks the following optimization:

$$U_{\text{opt}} = \arg \max_U \sum_{k=1}^m \frac{|H_\Gamma \cap H_{\Upsilon_k}^U|}{|H_\Gamma|}. \quad (11)$$

Thus,  $U_{\text{opt}}$  should maximize the intersection of  $H_\Gamma$  and  $H_{\Upsilon_k}^U$ . However, (11) only measures a global property of the similarity between the centroid sets.

Our second goal serves as a complementary of the problem. Because  $\Upsilon_k$  is a subset of  $\Gamma$ , we can find the centroids which simultaneous belong to  $\Gamma$  and  $\Upsilon_k$ . Therefore, we have  $x'_j = y_{kj}, x'_j \in \Gamma (j = 1, 2, \dots, n_k)$ . In  $\Gamma$ , we center a ball with radius  $r$  on  $x'_j$ , the number of the centroids in this ball

are regarded as  $N_{(x'_j, r)}^U$ . Similarly, in  $\Upsilon_k$ , the number of the centroids in the ball centered at  $y_{kj}$  with radius  $r$  is  $N_{(y_{kj}, r)}^U$ . The second goal pursuits that the ratio  $N_{(x'_j, r)}^U/|\Gamma|$  should be approximately equal to the ratio  $N_{(y_{kj}, r)}^U/|\Upsilon_k|$  as much as possible. Therefore, the second goal tries to optimize the mathematical problem

$$U_{\text{opt}} = \arg \min_U \sum_{k=1}^m \sum_{j=1}^{n_k} \left| N_{(x'_j, r)}^U/|\Gamma| - N_{(y_{kj}, r)}^U/|\Upsilon_k| \right|. \quad (12)$$

Though the total number of elements in  $\Upsilon_k$  is smaller than that in  $\Gamma$ , the difference between the ratios can be as small as possible.

We incorporate global and local measurements into the same objective function. Then the mathematical model of the second fact is

$$U_{\text{opt}} = \arg \min_U \frac{\sum_{k=1}^m \sum_{j=1}^{n_k} \left| N_{(x'_j, r)}^U/|\Gamma| - N_{(y_{kj}, r)}^U/|\Upsilon_k| \right|}{\sum_{k=1}^m |H_\Gamma \cap H_{\Upsilon_k}^U|/|H_\Gamma|}. \quad (13)$$

The objective functions of (8) and (13) are difficult to optimize directly. However, this problem can be regarded as an optimization problem of the discrete centroids. Therefore, it is of importance to evaluate the relations between the centroids of a subset and the relations between the centroids of different subsets.

### B. Proposed Solution—LBWCMD

With the two facts we have mentioned, actually our problem is to maximize the distances between the centroids in a subset and minimize the distances between the centroids in different subsets. This problem is quite different from the clustering problems [26] we have seen commonly. In this paper, we propose a lower bound-based measurement to describe the distance between the two centroids from the same subset or different subsets so as to obtain a reasonable solution of the problem. For the well-known  $k$ -mean method [26], to accomplish the clustering task, it needs to answer the following two questions after the initialization: 1) which sample in the class should be removed and 2) which class should the removed sample be added to? Follow the same procedures as  $k$ -mean but rather different intrinsic principles, we demonstrate the proposed method as follows. First, we initialize  $m$  subsets of the centroid set  $\Gamma$ . Then, for the centroids in a subset, we have to tackle with the following two problems: 1) which centroid should be the candidate that has to be transferred to another subset and 2) which subset should the centroid be assigned to when the centroid has to be transferred?

For the first problem, we propose to use a ball centered at a centroid with radius  $r$  to determine whether this centroid should be excluded from the subset. With the first fact, adjacent centroids should be assigned to different subsets. Let  $n_i$  be the number of the centroids in the  $i$ th subset ( $i = 1, 2, \dots, m$ ). Let  $x_{ij} = (x_{ij}^1, x_{ij}^2)$  be the  $j$ th centroid in the  $i$ th subset,  $j = 1, 2, \dots, n_i$ . Define a ball set  $\Lambda_{ij} = \{b \mid (b_1 - x_{ij}^1)^2 + (b_2 - x_{ij}^2)^2 \leq r^2\}$  for  $x_{ij}$ , where  $b = (b_1, b_2)$

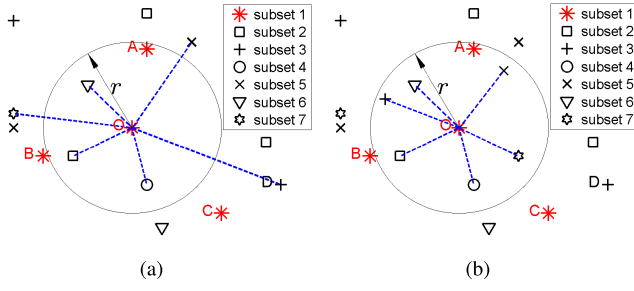


Fig. 5. Centroids are distributed to seven subsets. (a)  $r$ -ball of centroid O contains centroid A from the same subset. (b) Situation which meets the first restriction but not the second one, namely  $r$ -ball of centroid O contains the centroids from all subsets.

is a centroid inside the ball. A centroid  $x_{ij}$  should be removed only if the following two restrictions are satisfied:

- 1) the first restriction is  $\{x_{iq}\} \neq \emptyset$ ,  $x_{iq} \in \Lambda_{ij}$  and  $q \neq j$ ;
- 2) the second restriction is  $|\{x'_{pq}\}| < m - 1$ ,  $x'_{pq} \in \Lambda_{ij}$

$$x'_{pq} = \arg \min_q \|x_{ij} - x_{pq}\| \quad (14)$$

and  $p \neq i$ .

The first restriction shows that some centroids that are from the same subset as  $x_{ij}$  fall into an  $r$ -ball of  $x_{ij}$ . Therefore,  $x_{ij}$  is the candidate that should be removed so as to maintain the space structure of the centroids in the  $i$ th subset, that is, no more than two centroids from the same subset can coexist in the  $r$ -ball. However, the second restriction guarantees that at least one subset is available for  $x_{ij}$  to be transferred to, meanwhile the space structure of the centroids in this subset is well maintained. Optimization problem of (14) obtains all the centroids that are the nearest to  $x_{ij}$  from other subsets. The second restriction shows that these centroids are in the  $r$ -ball of  $x_{ij}$ . However, if all the subsets have the centroids (the nearest one to  $x_{ij}$  in each subset) in the  $r$ -ball of  $x_{ij}$ , namely  $\{\{x'_{pq}, p = 1, 2, \dots, m\} \cup x_{ij}\} \subset \Lambda_{ij}$ , it is not necessary to transfer centroid  $x_{ij}$  to another subset. Because, in such a situation, two centroids of a subset will be in an  $r$ -ball. Therefore, we need additional restriction  $|\{x'_{pq}\}| < m - 1$  and  $p \neq i$ . In Fig. 5(a), seven subsets have been initialized. The  $r$ -ball of centroid O contains centroid A that comes from the same subset as centroid O. So centroid O is the candidate that should be removed. In addition, subsets 1, 2, 4, and 6 have the centroids in the  $r$ -ball of centroid O and not less than three subsets have no centroid in the  $r$ -ball. Hence, centroid O should be removed from subset 1. However, Fig. 5(b) shows a situation which meets the first restriction but not the second one. Therefore, in such a situation, centroid O should not be removed.

For the second problem, based on the second fact, we need to guarantee the motion of each subset comes from the whole scene. Therefore, for the centroids in a subset, the within-class distances should be maximized. We propose to assign centroid  $x_{ij}$  to the  $p$ 'th subset with the condition,  $\{x_{p,q}\} \cap \Lambda_{i,j} = \emptyset$

$$p' = \arg \max_p \min_q \|x_{i,j} - x_{p,q}\| \quad (15)$$

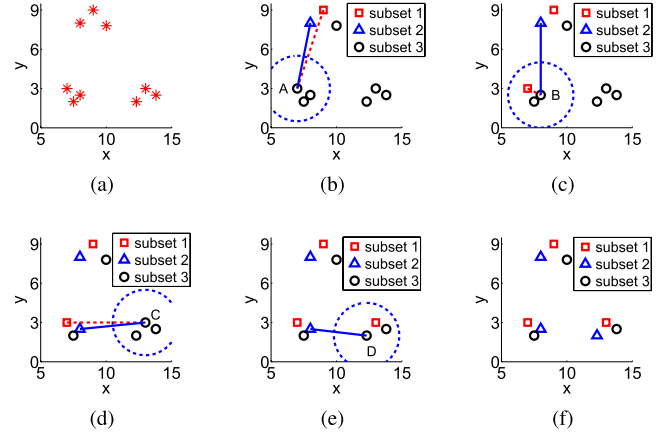


Fig. 6. Concise demo of LBWCMD. (a) Original distribution of the centroids. (b) We first initialize the states of the centroids. According to LBWCMD, centroids A, B, C, and D become square, triangle, square, and triangle markers, respectively, as shown in (c), (d), (e), and (f).

and  $p \neq i$ . The formulas  $\{x_{p,q}\} \cap \Lambda_{i,j} = \emptyset$  and  $p \neq i$  try to exclude the existing subsets in which the centroids fall into the  $r$ -ball of  $x_{i,j}$ . To determine an optimal subset that the selected centroid  $x_{ij}$  should be assigned to, we consider the remaining subsets which contain the centroids outside the  $r$ -ball of  $x_{i,j}$ . We rank these subsets in a descending order based on the distances between  $x_{i,j}$  and each subset. The top ranking subset, namely the  $p$ 'th subset, is the best selection. The dashed lines in Fig. 5(a) show the nearest distances between centroid O and other subsets. Among all the nearest distances, the one between centroid O and centroid D is the largest. Using the within-class maximum principle, centroid O should be assigned to subset 3. The details of the method are described in Algorithm 1. The proposed LBWCMD method can assign successive frames to different subsets by a lower-bound strategy which gives an approximate solution to (8). Moreover, this method ensures that the spatial distribution of each centroid subset meets (13) as much as possible.

We now give a concise demo to demonstrate the main steps of LBWCMD method. Fig. 6(a) shows several centroids for division. Let  $m = 3$ ,  $r = 2.5$ . According to step 1 of LBWCMD, the  $i$ th centroid is assigned to the  $i$ th division,  $i = 1, 2, \dots, m - 1$ , and the rest of the centroids are assigned to the  $m$ th subset as shown in Fig. 6(b). Suppose that the centroids with the square marker are from the first subset, the ones with the triangle marker are from the second subset and the ones with the circle marker are from the third subset. According to steps 8–19 of Algorithm 1, centroid A is assigned to the farthest subset outside  $r$ -bound of centroid A. As shown by the dash line in Fig. 6(b), centroid A should be assigned to the first subset. Then, we go through centroid B, C, and D based on the same idea. Similarly, the division results are shown in Fig. 6(c)–(f), respectively. Fig. 6(f) shows that the proposed method not only separates adjacent centroids to different subsets, but also enable each subset to maintain almost the same spacial distribution as the original centroid set.

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**Algorithm 1** Lower Bound-Based Within-Class Maximum Division (LBWCMD)

---

**Input:**  $X \in \mathbb{N}^{p \times n}$ , number of subsets  $m$ , lower bound  $r$ , initial values for number of iterations  $u = 0$ , thresh  $T = 20$ , flag  $b = 0$ , constant  $\tau = 5$

1: Initialization:

$$N_t(i) \leftarrow \begin{cases} 1 & i = 1, 2, \dots, m-1 \\ n - (m-1) & i = m \end{cases},$$

$$L(j) \leftarrow \begin{cases} j & j = 1, 2, \dots, m-1 \\ m & j = m, m+1, \dots, n \end{cases}.$$

2: **while**  $b$  equals to 0 and  $u < T$  **do**

3: **for**  $i = 1, 2, \dots, m$  **do**

4: **if**  $N_t(i) \leq 1$  **then** continue. **end if**

5: Extract samples with label  $i$  from  $X$  to obtain  $Y_i$ .

6:  $N_{Y_i} = N_t(i)$ ;

7: **for**  $j = 1, 2, \dots, N_{Y_i}$  **do**

8: Extract the  $j$ th sample from  $Y_i$  to obtain  $x_j$ .

9:  $d = \arg \min_{d_p} d_p$ , s.t.  $d_p = \|x_j - x_p\|$ ,  $p = 1, 2, \dots, N_{Y_i}$  and  $p \neq j$ .

10: **if**  $d \leq r$  **then**

11:  $d_c(k) = \arg \min_{d_k} d_k$ , s.t.  $d_k = \|x_j - y_{kq}\|$ ,  $y_{kq}$  is the  $q$ th sample from the  $k$ th subset,  $k = 1, 2, \dots, m$ ,  $k \neq i$ .

12:  $s = \sum_{k=1,2,\dots,i-1,i+1,\dots,m} \delta(r - d_c(k))$ ,

$$\delta(x) = \begin{cases} 1 & x \geq 0 \\ 0 & x < 0 \end{cases}.$$

13:  $l = \arg \max_k d_c(k)$ ,  $k = 1, 2, \dots, m$  and  $k \neq i$ .

14: **if**  $s < m - 1$  or  $|N_{Y_i} - N_{Y_l}| < \tau$  **then**

15:  $N_t(i) \leftarrow N_t(i) - 1$ .

16:  $L(j) \leftarrow l$ .

17:  $N_t(l) \leftarrow N_t(l) + 1$ .

18: **end if**

19: **end if**

20: **end for**

21: **end for**

22:  $d_g(k) = \arg \min_{d_k} d_k$ ,  $d_k = \|y_{kp} - y_{kq}\|$ ,  $y_{kj}$  is the  $j$ th sample from the  $k$ th subset,  $k = 1, 2, \dots, m$ ,  $p, q = 1, 2, \dots, N_t(k)$  and  $p \neq q$ .

23:  $s = \sum_{k=1,2,\dots,m} \delta(d_g(k) - r)$ .

24: **if**  $s$  is equal to  $m$  **then**  $b = 1$ . **end if**

25:  $u \leftarrow u + 1$ .

26: **end while**

**Output:**  $N_t, L$ .

---

Using the proposed LBWCMD method, we can map the corresponding frames to the division set  $P_i (i = 1, 2, \dots, m)$  according to the already known centroid subsets.

## V. AUGMENTED SET CONSTRUCTION

Although we have finished the construction of the basic sets. It is not yet ready to carry on RPCA on these basic sets.

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**Algorithm 2** Augmented Set Construction (ASC)

---

**Input:** Basic set  $X_i$ , foreground set  $\{f_j\}$ , and its corresponding area  $s_j, j = 1, 2, \dots, n$ , initial values for  $\alpha, Y_i = \emptyset, i = 1, 2, \dots, m$ .

1. Sort  $\{f_j\}$  based on  $s_j$  in ascending order to obtain

$$\{f_{k_j} | s_{k_1} \leq s_{k_2} \leq \dots \leq s_{k_n}, j = 1, 2, \dots, n\}.$$

2. Select the top  $\lfloor \alpha \times n \rfloor$  frames to construct set  $M = \{f_{k_j}\}, j = 1, 2, \dots, \lfloor \alpha \times n \rfloor$ .

3. **for**  $j = 1, 2, \dots, \lfloor \alpha \times n \rfloor$  **do**

4. **for**  $i = 1, 2, \dots, m$  **do**

5. **if**  $f_{k_j} \notin X_i$  **then**

6.  $Y_i \leftarrow Y_i \cup \{f_{k_j}\}$ .

7. **end if**

8. **end for**

9. **end for**

**Output:**  $Y_i, i = 1, 2, \dots, m$ .

---

First, the scale of each basic set is much smaller than ever before, which results in an insufficient number of frames for the low-rank decomposition. Second, there are still more possibilities for us to make full use of the motion *priori* knowledge. In this section, we propose to construct an augmented set as a supplementation for each basic set. To this end, the frames with a small quantity of motion will be selected. Let  $s_j$  be the area of the binary foreground  $f_j$  of the  $j$ th frame,  $j = 1, 2, \dots, n$ . Based on  $s_j$ , we sort the foreground in ascending order to obtain  $\{f_{k_j} | s_{k_1} \leq s_{k_2} \leq \dots \leq s_{k_n}, j = 1, 2, \dots, n\}$ , where the top  $\lfloor \alpha \times n \rfloor$  frames are selected to construct set  $M = \{f_{k_j} | j = 1, 2, \dots, \lfloor \alpha \times n \rfloor\}$  that composed of the frames with a small quantity of motion. Let  $Y_i$  be the augmented set which is corresponding to basic set  $X_i, i = 1, 2, \dots, m$ .  $Y_i$  includes the frames in  $M$  but not in  $X_i$ . Therefore,  $Y_i$  acts as a supplementation to the basic set. The details for constructing the augmented sets are summarized in Algorithm 2.

Ultimately, we divide  $\Omega$  into  $Z_1, Z_2, \dots, Z_m$ , namely  $\Omega = \bigcup_{i=1,2,\dots,m} Z_i$ , where  $Z_i = X_i \cup Y_i$ . The full name of the whole framework is Joint Video Frame Set Division and RPCA-based background subtraction (JVFS-D-RPCA) which is described in Algorithm 3.

## VI. PARAMETER TUNING OF $\alpha$

The proposed LBWCMD consists of three parameters, namely  $m, r$ , and  $\alpha$ .  $m$  indicates the number of divisions of video frame set.  $r$  describes the distance between the locations of two people. We will consider the values of these two parameters in the next section. For the third parameter  $\alpha$ , it reflects the number of frames with slight motion. The larger the  $\alpha$  is, the more these types of frames exist. Our rule for setting the value of this parameter is as follows. Define a step function

$$g(x) = \begin{cases} 1, & x < 0 \\ 0, & x \geq 0 \end{cases} \quad (16)$$

Let  $\text{Area}(F^{(i)})/wh$  stand for the ratio of the foreground pixel to all the pixels in the frame, where  $F^{(i)}$  is the  $i$ th foreground



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**Algorithm 3** Joint Video Frame Set Division and RPCA-Based Background Subtraction (JVFS-RPCA)

---

**Input:**  $n$  video frames  $I^{(k)} \in \mathbb{N}^{h \times w}$ , number of partitions  $m$ , lower bound  $r$ , initial values for  $\alpha$ .

1. Use the proposed method in Section III to obtain centroid set  $\Phi$  which consists of the centroids of major moving objects in all frames and set  $Q$  with nonmotion frames.
2. Put the centroids in  $\Phi$  as column vectors of data matrix  $X$ . Take  $X$  as input for **Algorithm 1 (LBWCMD)** to assign the centroids to  $m$  divisions. Then we have division set  $P_i, i = 1, 2, \dots, m$ .
3. Divide  $Q$  into  $m$  subsets  $Q_i, i = 1, 2, \dots, m$ . Merge  $P_i$  and  $Q_i$  to obtain basic set, namely  $X_i = P_i \cup Q_i$ . The index of frames in  $X_i$  is  $\{l_{ij} | j = 1, 2, \dots, |X_i|; i = 1, 2, \dots, m\}$ .
4. Use **Algorithm 2 (ASC)** to construct the augmented set  $Y_i$  and merge it with the basic set  $X_i$  to obtain the group set  $Z_i = X_i \cup Y_i$ .
5. Run RPCA on each group set  $Z_i$  to isolate the corresponding background and foreground for each frame.

**Output:** Background set  $\{B_{l_{ij}}\}$  and foreground set  $\{F_{l_{ij}}\}, j = 1, 2, \dots, |X_i|; i = 1, 2, \dots, m$ .

---

which is estimated by the method used in Section III. Therefore, the ratio of the number of these types of frames to  $n$  is

$$f(x) = \frac{1}{n} \sum_{i=1}^n \left[ g \left( \frac{\text{Area}(F^{(i)})}{wh} - \epsilon \right) \right]. \quad (17)$$

Then, we define

$$\alpha = \begin{cases} f(x), & f(x) > \delta \\ \delta, & f(x) \leq \delta. \end{cases} \quad (18)$$

It means that the proposed method pursues the frames with slight motion as much as possible.

## VII. EXPERIMENTAL RESULTS

In this section, two groups of experiments were used to evaluate the effectiveness of JVFS-RPCA and a detailed complexity analysis of the proposed method was given. Because the LBWCMD method is the core of our method, in the first group of experiment, we created four kinds of artificial point sets to test the performance of LBWCMD. In the second group of experiment, we compared JVFS-RPCA with the state-of-the-art subspace-based background subtraction methods, including robust principle component analysis (RPCA) [19], go decomposition (GoDec) [24], principle component analysis (PCA) [17], and robust principle component analysis with M-estimation (RPCA-ME) [18]. Moreover, we also compared the proposed method with the statistic-based, classification-based, and nonparametric methods, including Mahalanobis distance (MD) [27], improved gaussian mixture model (GMM) [28], self-organizing-based method (SOBS) [14], and kernel density estimation (KDE) [10]. All the comparisons will be conducted on real-world and public sequences.

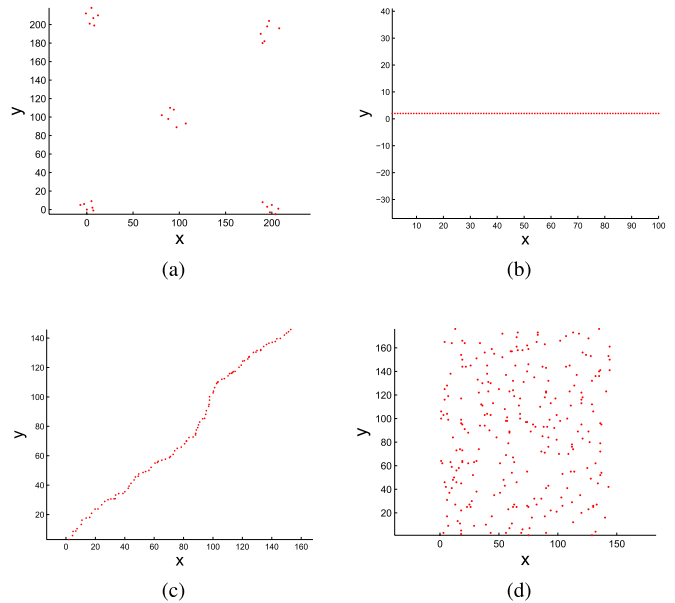


Fig. 7. Artificial point sets for division. (a) Decentralized assembled points. (b) Straight walking points. (c) Random walking points. (d) Uniformly distributed points.

TABLE III  
PARAMETER SETTING FOR THE POINT SET DIVISION

Point set	Value of $m$	Value of $r$
Decentralized assembled points	6	70
Straight walking points	4	3
Random walking points	4	5
Uniformly distributed points	6	28

### A. Experiments on Artificial Point Sets

For a certain point set, the proposed LBWCMD method can maximize the within-class distances while maintaining the spatial distribution in each subset. In this section, we created four artificial point sets to validate it. The point sets include the decentralized assembled points, straight walking points, random walking points, and uniformly distributed points, which are shown in Fig. 7(a)–(d). We also used the objective function values of (11)–(13) to evaluate the performance of LBWCMD.

The lower bound  $r$  plays an important role in LBWCMD. It decides the minimum distance between the two points from the same subset. If  $r$  is too small, the points cannot be assigned to different subsets as much as possible. On the contrary, if  $r$  is too big, there will be an unbalance number of the points in the subsets. Therefore, a proper value of  $r$  should be used. In this experiment, we used the parameters in Table III to divide the point sets.

The division results are shown in Fig. 8. Obviously, the adjacent points can be assigned to different subsets while the spatial distribution of each subset is well maintained. We can see some numerical results in Table IV. It shows that the convex hull of each subset largely overlaps with that of the original point set except for subset 4 of the random walking point set. Because some of the points in the random



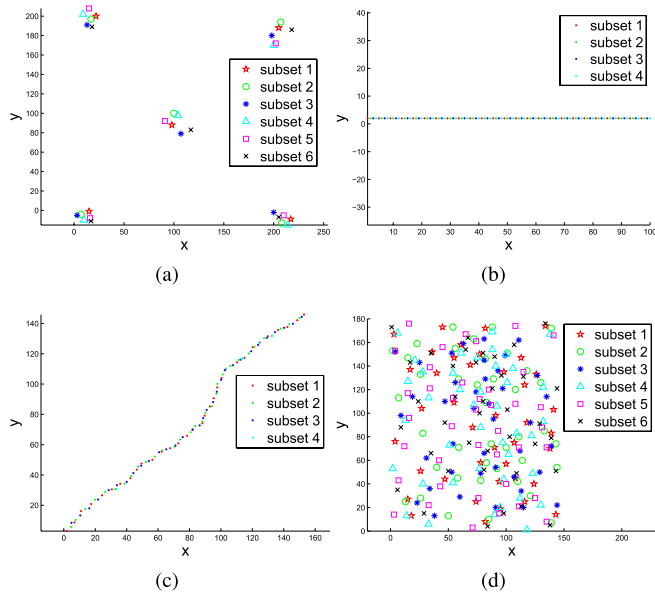


Fig. 8. Results of LBWCMD on the point sets. The division results of (a) decentralized points, (b) straight walking points, (c) random walking points, and (d) uniformly distributed points.

TABLE IV  
EFFECTIVENESS OF LBWCMD ON THE POINT SETS

		Decentralized assembled points	Straight walking points	Random walking points	Uniformly distributed points
Global similarity in (11) for all subsets	subset 1	84.90%	97.00%	91.75%	84.11%
	subset 2	88.49%	97.00%	86.31%	89.13%
	subset 3	80.12%	97.00%	85.70%	77.90%
	subset 4	86.63%	97.00%	24.14%	85.82%
	subset 5	82.87%	—	—	87.80%
	subset 6	84.54%	—	—	86.55%
Local similarity in (12)		0	2.88	2.19	6.71
Objective function value of (13)		0	0.74	0.76	1.31

walking point set are not well aligned. In addition to the global similarity, the local similarity related to the point sets is well obtained. A comprehensive evaluation of the effectiveness of LBWCMD is shown in the last row in Table IV. The smaller the objective function value of (13) is, the better subsets we had obtained. Among all the objective function values, only one of the uniformly distributed point set is the worst. The main reason is that some badly aligned points are not well handled. Nevertheless, it is concluded from the overall results that the proposed method is feasible to make a good division to the point sets.

### B. Experiments on Video Data Sets

In this section, we conducted the experiments on 11 real-world and public sequences. The sequences include three challenging ones (*Fighting* and two *Walking with occlusion* sequences) captured by ourselves (the corresponding ground truths can be downloaded at <http://www.yongxu.org/lunwen.html>), *Intelligent room* [29], three sequences (*Water-Surface*, *Meeting room*, *Switch light*) from Li's Data Set [37],

two sequences (*Highway*, *Pedestrians*) from Change Detection Data Set [31], *Dance bootstrapping* from Competition data set [32] and *Pets 2006 S7* [25]. We compared JVFSD-RPCA with RPCA [19], GoDec [24], PCA [17], RPCA-ME [18], MD [27], SOBS [14], GMM [28], and KDE [10]. The source codes of RPCA, GoDec, and RPCA-ME can be downloaded at [33], [34], and [35], respectively. Oliver *et al.* [17] did not provide the source code of PCA for background subtraction. Hence, we implemented this code by ourselves. The source codes of MD, SOBS, GMM, and KDE can be downloaded at the website of BGSLibrary [36].

In these experiments, all the ground truths of the frames were used to evaluate the performances of the methods. If the detected regions are included in the ground truth, they are true positive, otherwise they are false positive. We adopted the similarity measurement used in [37] to evaluate the performances of the methods. Let  $D$  be a detected region and  $G$  be the ground truth on the corresponding frame. The similarity measurement between  $D$  and  $G$  is defined as

$$S(D, G) = \frac{D \cap G}{D \cup G}. \quad (19)$$

If the detected foreground is exactly the same as the ground truth, the similarity approaches to 1. On the contrary, if the detected foreground has no overlap with the ground truth, the similarity approaches to 0. Therefore, we can conveniently evaluate the performance of JVFSD-RPCA and other methods with similarity measurement (19).

1) *Parameters Setting*: For our method, three parameters need to be determined, namely  $m$ ,  $r$ , and  $\alpha$ . We used  $m = 10$  and  $r = 6$  for all the sequences.  $\alpha$  can be determined by (18) with empirical values  $\epsilon = 0.01$  and  $\delta = 0.05$ . For RPCA, as mentioned in [19], the suggested value of  $\lambda$  is  $1/(\max(wh, n))^{1/2}$ , where  $w$  and  $h$  are the width and height of the frame. However, we discovered that the suggestion does not work in our experiments. To this end, we multiplied  $\lambda$  by a weight  $\rho$  so as to make a proper balance between the low-rank and sparse components. Hence we obtained  $\lambda$  by

$$\lambda = \frac{\rho}{\sqrt{\max(wh, n)}} \quad (20)$$

where  $\rho = 0.06$ . For GoDec, we set the rank of measurement matrix to 2 and used the default values of the iteration parameters in the algorithm. For RPCA-ME and PCA, the number of principle components was set to 10. Because these subspace-based methods are of the batch types for dealing with the coming frames, we used every 300 frames to construct the measurement matrix for background subtraction. After the foreground had been extracted by the subspace-based methods, a threshold of 25 was adopted to convert the results into binary images. For the MD method, the sensitivity, noise variance, and learning rate were set to 100, 150, and 30, respectively. For SOBS method, the training sensitivity, learning rate in training phase, and training steps were set to 245, 255, and 55 while the testing sensitivity and learning rate in testing phase were set to 130 and 62, respectively. For the GMM method, three Gaussian models were used and the learning rate was set to 0.008. For KDE method, the window size was set to 100.

TABLE V  
AVERAGE SIMILARITIES (%) ON DIFFERENT SEQUENCES

Sequence	JVFS-D-RPCA	RPCA	GoDec	RPCA-ME	PCA	MD	SOBS	GMM	KDE
<i>Fighting</i>	<b>57.26</b>	48.27	17.32	41.37	37.69	35.74	22.61	36.04	42.09
<i>Intelligent room</i>	<b>64.33</b>	63.38	61.76	45.27	26.96	28.31	63.92	31.67	63.17
<i>WaterSurface</i>	<b>76.84</b>	32.08	76.12	20.70	9.18	50.49	76.46	32.13	74.67
<i>Meeting room</i>	70.40	42.00	<b>71.91</b>	37.47	22.37	45.62	51.36	38.75	41.90
<i>Highway</i>	<b>67.76</b>	64.60	15.17	54.25	48.06	46.07	53.98	67.10	47.10
<i>Dance bootstrapping</i>	89.09	<b>89.22</b>	15.57	74.56	46.61	79.70	51.17	76.06	46.79



Fig. 9. Comparison results on different sequences. First to sixth rows: Detection results on 221th frame of *Fighting*, 216th frame of *Intelligent room*, 1615th frame of *WaterSurface*, 23857th frame of *Meeting room*, 1615th frame of *Highway*, and 338th frame of *Dance bootstrapping* sequences. First and second columns: Original image and its ground truth. Third to eleventh columns: Results of JVFS-D-RPCA, RPCA, GoDec, RPCA-ME, PCA, MD, SOBS, GMM, and KDE, respectively.

2) *Experiments on Different Environments*: In this section, we compared the performances of the aforementioned methods on different environments including four indoor sequences (*Fighting*, *Intelligent room*, *Meeting room*, and *Dance bootstrapping*) and two outdoor sequences (*WaterSurface* and *Highway*). The *Fighting* sequence was captured by ourselves with the length of 300. We labeled the ground truths of the frames on every 10 frames. The resolution with  $352 \times 288$  was used for the experiment. The *Intelligent room* sequence has a length of 300 and a resolution of  $320 \times 240$ . According to [29], the frames range from 82 to 299 are provided with ground truths when the person starts to walk into the room. The *WaterSurface* and *Meeting room* sequences contain dynamic backgrounds. The former is of the length of 633 and the latter is of the length of 2964. Both sequences are in the resolution of  $160 \times 128$ . According to [37], for each sequence, 20 ground truths are provided on the key frames to evaluate the performances of the algorithms. The *Highway* sequence has a length of 1700 and a resolution of  $320 \times 240$ . The ground truths are provided in the range of 470–1700. For the *Dance bootstrapping* sequence, it has a length of 747 with the resolution of  $384 \times 240$ . All the ground truths of the frames are provided. We ran nine algorithms on six sequences. The results of the average similarities on

the sequences are shown in Table V. The results in bold font highlight the highest average similarity among all the methods on the same sequence. The proposed JVFS-D-RPCA outperforms other methods on four sequences. In another two sequences, the competitiveness of our method is almost the same as GoDec on *Meeting room* sequence and RPCA on *Dance bootstrapping* sequence. Some examples of the foreground extraction results are shown in Fig. 9. The second column shows the ground truth of the corresponding frame. Our result is shown in the third column. We can see that the proposed method performs well on all the sequences. However, some of the algorithms, like RPCA-ME, PCA, and GMM do not work well on *WaterSurface* and *Meeting room* sequences. RPCA works well on most of the sequences. However, if the moving objects stay for a while in a fixed location of the scene, RPCA cannot extract the entire foreground of the object. Differ from RPCA, the proposed JVFS-D-RPCA pursues the sparsity not only in space but also in time and exploits the frames with slight motion to provide more genuine background pixels for low-rank decomposition. With these situations, JVFS-D-RPCA is much more competitive than RPCA. In the eighth and the eleventh columns of Fig. 9, we can find that the MD method is quite sensitive to noises and KDE cannot perform well on *Meeting room*, *Highway*, and *Dance bootstrapping*.

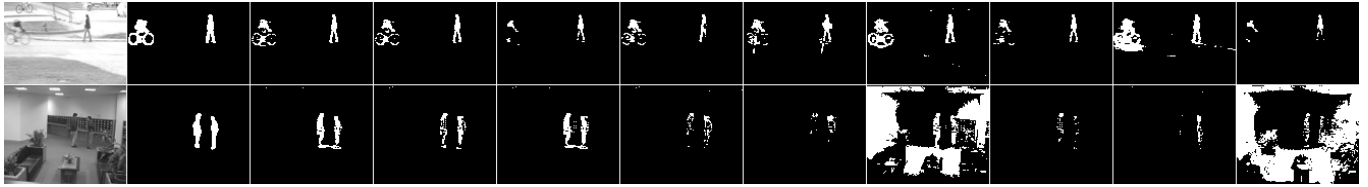


Fig. 10. Comparison results on strong lighting sequences. First to second rows: Detection results on 467th frame of *Pedestrians* and 2507th frame of *Switch light* sequences. First and second columns: Original image and its ground truth. Third to eleventh columns: Results of JVFSR-RPCA, RPCA, GoDec, RPCA-ME, PCA, MD, SOBS, GMM, and KDE, respectively.

TABLE VI  
AVERAGE SIMILARITIES (%) ON STRONG LIGHTING SEQUENCES

Sequence	JVFSR-RPCA	RPCA	GoDec	RPCA-ME	PCA	MD	SOBS	GMM	KDE
<i>Pedestrians</i>	<b>73.66</b>	73.53	52.53	72.77	58.41	65.25	66.14	72.07	48.84
<i>Switch light</i>	<b>61.68</b>	57.23	59.32	38.23	29.23	11.09	23.14	36.20	8.36

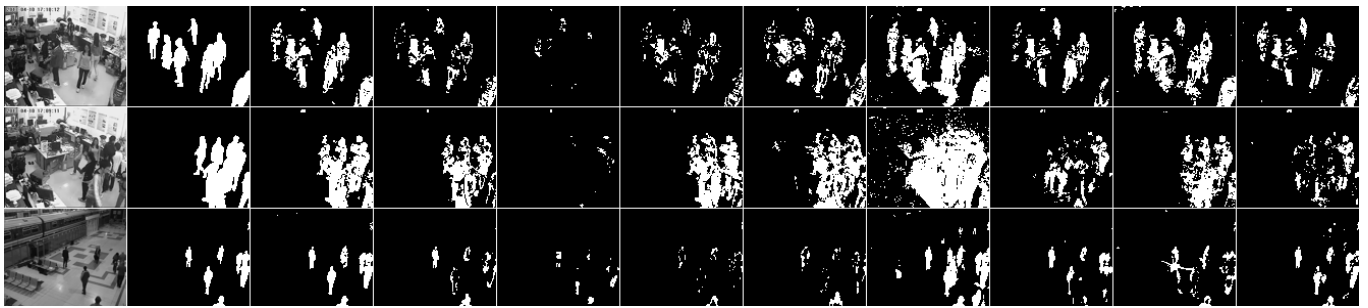


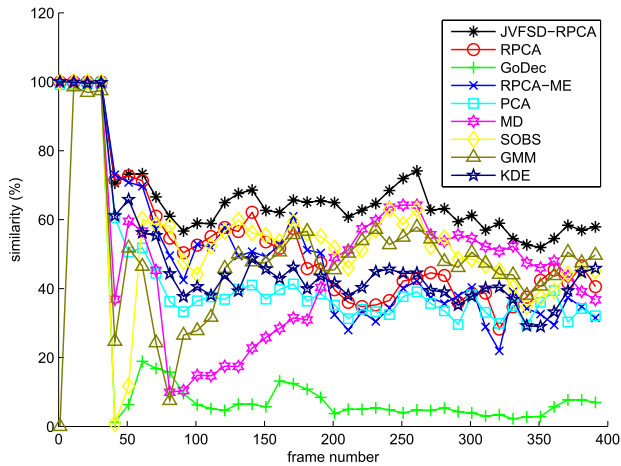
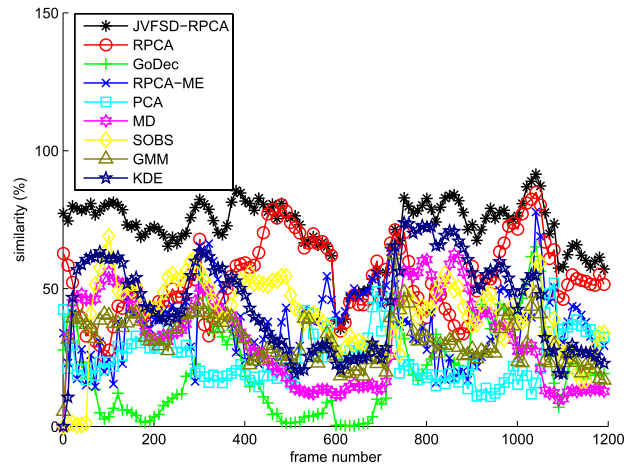
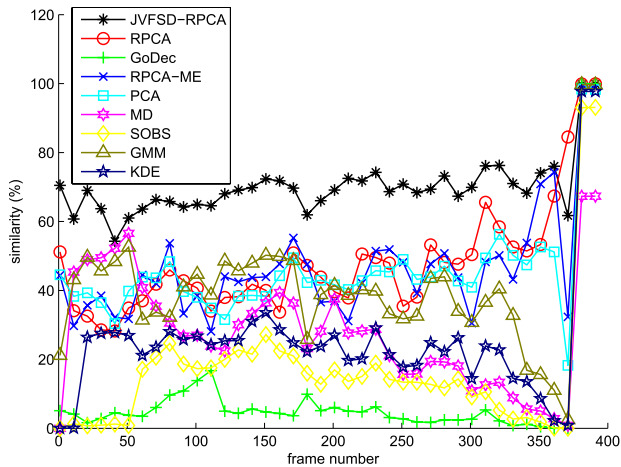
Fig. 11. Comparison results on challenging sequences with serious occlusion. First to third rows: Detection results on 211th frame of *Walking I*, 171th frame of *Walking II*, and 841th frame of *Pets 2006 S7* sequences. First and second columns: Original image and its ground truth. Third to eleventh columns: Results of JVFSR-RPCA, RPCA, GoDec, RPCA-ME, PCA, MD, SOBS, GMM, and KDE, respectively.

TABLE VII  
AVERAGE SIMILARITIES (%) ON CHALLENGING SEQUENCES

Sequence	JVFSR-RPCA	RPCA	GoDec	RPCA-ME	PCA	MD	SOBS	GMM	KDE
<i>Walking I</i>	<b>66.45</b>	52.68	16.02	49.28	43.46	47.67	53.98	47.74	48.43
<i>Walking II</i>	<b>68.89</b>	47.91	9.34	46.44	45.18	27.80	16.18	40.05	24.89
<i>Pets 2006 S7</i>	<b>71.82</b>	53.68	20.22	37.05	25.07	32.27	40.43	31.16	44.60

3) *Experiments on Strong Lighting Sequences:* In this section, we evaluated the algorithms under strong lighting situations. Two sequences were used for testing. One is an outdoor *Pedestrians* sequence with strong lighting. The sequence has a length of 1099 and a resolution of  $360 \times 240$ . The other is an indoor *Switch light* sequence which first turns off the light and then turns on the light causing strong lighting changes. The sequence is with the length of 1546 and resolution of  $160 \times 128$ . *Pedestrians* sequence provides the ground truths in the range of 300–1099 and *Switch light* sequence provides 20 ground truths of the key frames for performance evaluation according to [37]. We performed all the algorithms on the two sequences. The average similarities results are shown in Table VI. Our method obtains better foreground extraction results than the other methods. See the second row in Fig. 10, RPCA-ME, PCA, SOBS, and GMM do not obtain good results under the situation of *Switch light*. MD and KDE are much more sensitive to lighting changes comparing with other methods.

4) *Experiments on Challenging Sequences With Serious Occlusion:* To further evaluate the performances of all the algorithms, we used three challenging sequences for the experiments. Two *Walking with occlusion* sequences were captured by ourselves. Both sequences are of the length of 400 and have a resolution of  $352 \times 288$ . We labeled the ground truths on every 10 frames. The *Walking I* and *Walking II* sequences are shown in the first and second rows of Fig. 11. The third sequence is *Pets 2006 S7* with a length of 1200 and a resolution of  $360 \times 288$ . This sequence is the most challenging one among all the seven sequences in *Pets 2006* Dataset. Many people appear in the scene. Moreover, the occlusion between the people happens quite often. Because no ground truths of this sequence are provided, we labeled the ground truths on every 10 frames and totally used 120 ground truths for evaluation. The detailed testing results of all the methods on *Walking I*, *Walking II*, and *Pets 2006 S7* sequences are shown in Figs. 12–14. It can be seen from three similarity curves that JVFSR-RPCA outperforms other methods among most

Fig. 12. Comparison results on *Walking I*.Fig. 14. Comparison results on *Pets 2006 S7*.Fig. 13. Comparison results on *Walking II*.

of the frames with ground truths. *Walking II* sequence has the most serious occlusion phenomenon among three challenging sequences. Even under such a situation, JVFSO-RPCA still can obtain a satisfactory result. However, the performances of other methods drop down as shown in Fig. 13. The average similarities of all the algorithms on three sequences are listed in Table VII which validate the effectiveness of JVFSO-RPCA on challenging sequences with serious occlusion. More vivid demonstration of the foreground extraction results can be seen in Fig. 11.

We present the rational explanation of the experimental results as follows. The subspace-based methods take all the successive frames as adjacent column vectors of a matrix and try to obtain the sparse component or outlier of this matrix. It can be regarded as a global scheme for background subtraction. However, in the crowded sequence, the background does not appear frequently owing to the highly dense walking flow. The global scheme fails when it comes to this situation. Unlike the global scheme, the JVFSO-RPCA considers the motion *priori* knowledge, then the proposed LBWCMD method can assign the successive frames to different subsets. Therefore, the frames in each subset are not continuous, which means

TABLE VIII  
FLOPS OF THE MAIN STEPS IN ALGORITHM 1

Main steps in Algorithm 1	Flops
9	$3vN_{Y_i} - 3v - 1$
11	$3vn - m + 1 - 3vN_{Y_i}$
22	$\frac{3}{2}v \sum_{i=1}^m N_{Y_i}^2 - \frac{3}{2}vn - m$

the measurement matrix is not only sparse in space but also sparse in time. This can alleviate the influence of the highly dense movement to some extent. In addition, we augmented each subset by using the frames with a small quantity of motion. This also can provide more genuine background pixels and prompt good recovery results. For the other methods, they usually need a training or learning phase to produce suitable parameters to detect the foreground. However, good parameters are very hard to obtain under the situation with serious occlusion.

### C. Complexity Analysis of the Proposed Method

The proposed method is summarized in Algorithm 3, which consists of Algorithms 1 and 2. For Algorithm 1, the flops of the main steps are listed in Table VIII, where  $n$  is the number of samples,  $v$  is the dimension of a sample,  $m$  is the number of subsets,  $N_{Y_i}$  is the number of samples of the  $i$ th subset in a certain while loop, and  $T$  is the maximum iteration times within while loop. As the sample is the location of moving object,  $v = 2$ . Taking all the steps into consideration, the maximum complexity of Algorithm 1 is  $O(Tmn^2)$ . For Algorithm 2, the main complexity is produced in step 1 which consists of foreground pixel counting and foreground area sorting. The former costs  $O(nwh)$  and the latter costs  $O(n^2)$ , where  $h$  and  $w$  are, respectively, the height and width of an image. However, in our problem,  $wh \gg n$ . Therefore, The complexity of Algorithm 2 is  $O(nwh)$ . For Algorithm 3, the complexity of step 1 is easy to evaluate, namely  $O(nwh)$ . Steps 2 and 4 complexities are related to Algorithms 1 and 2, which have been discussed above. The complexity of step 3 is  $O(m)$ . Finally, we execute step 5 to run RPCA on each group set. The complexity of RPCA has been



TABLE IX  
AVERAGE EXECUTION TIMES (s) OF THE METHODS ON DIFFERENT SEQUENCES

Sequence	JVFSD-RPCA	RPCA	GoDec	PRCA-ME	PCA	MD	SOBS	GMM	KDE
<i>Intelligent room</i>	12.7	11.0	<b>17.9</b>	2.0	2.5	5.0	5.4	4.4	4.6
<i>Walking I</i>	19.8	19.3	<b>21.5</b>	2.8	3.4	7.3	7.7	6.7	6.9
<i>WaterSurface</i>	19.9	17.6	<b>25.6</b>	2.2	4.9	9.7	10.2	8.7	7.1
<i>Dance bootstrapping</i>	27.1	25.7	<b>33.2</b>	3.1	6.7	11.2	12.0	10.1	10.5

discussed in [21], namely  $O(nwh\min(n, wh))$ . In summary, the complexity of the proposed method is  $O(nwh\min(n, wh))$ . For other subspace-based methods, the complexity of GoDec, RPCA-ME and PCA is  $O(nwh\bar{r})$  [24],  $O(nwh\bar{k})$  [18], and  $O(n^3)$  where  $\bar{r}$  is the predefined low rank of measurement matrix and  $\bar{k}$  is the number of principle components of measurement matrix, respectively.

As the proposed method is based on RPCA, the pre-processing procedures have to be completed at first. Then RPCA is conducted on each group set  $Z_i (i = 1, 2, \dots, m)$  to extract the foregrounds. Although the complexity of the proposed method is of the same level as RPCA, the counting flops of the proposed method are more than RPCA. With the design of the proposed method as shown in Fig. 3(b), the executions of RPCA on the group sets are independent actually. Therefore, we can use parallel computing technique to accelerate the speed of the proposed method. For the sake of completeness, we compare the execution times of all the methods on Windows XP system with 3.4 GHz CPU and 8 GB RAM. The experiments were run 10 times over different sequences. The average execution times are listed in Table IX. The results in bold font highlight the longest execution time among all the methods on the same sequence. Obviously, the efficiency of GoDec is the lowest among all the methods. On the contrary, RPCA-ME holds the highest efficiency among all the methods. The proposed method runs about 1.5 s slower than RPCA on average. Because the proposed method has completed some optimization steps before RPCA, JVFSR-RPCA costs a little more time in background subtraction. Even though JVFSR-RPCA costs more time, experiments in 11 sequences show that our method is more competitive than the other methods.

### VIII. CONCLUSION

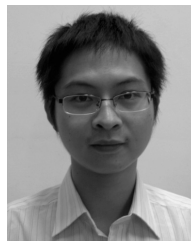
Unlike current subspace-based background subtraction methods, we took advantage of the motion *priori* knowledge and proposed a new JVFSR-RPCA method for background subtraction. The coarse motion estimation in Section III provides us the locations of the objects and the ratios of the foreground areas in the frames. With the centroids of the moving objects, we firstly developed LBWCMD method to divide the video frame set into different subsets for alleviating the influence of the highly dense movement. Then we constructed an augmented set using the frames with a small quantity of motion which facilitates us to obtain more genuine background pixels in each subset. By integrating the preceding two phases, we finally obtained the group sets, in which the moving objects are uniformly located at random. The proposed method makes the foreground pixels sparse not only in space but also in time.

Experiments on various challenging sequences validated the competitiveness of the proposed method comparing with the state-of-the-art background subtraction methods. The characteristics of the proposed method can be concluded from the experiments. First, LBWCMD can maintain the number of the frames in each subset at the same level. This is very important because the unbalanced scale of the subset will result in bad background extraction results. Second, JVFSR-RPCA works well in the situations of lighting changes or large size of occlusion such as sequence *Walking II*. However, some of the other methods fail in these situations. Third, the proposed method is an improved version of RPCA and it concentrates on enhancing the effectiveness of foreground detection results. Some optimization steps are completed before RPCA which results in more counting flops than RPCA. To make JVFSR-RPCA applicable, we can use the parallel computing technique to accelerate the speed of the proposed method. Experimental results in 11 sequences show that the proposed method is more competitive than the other methods. In the future, we will pay more attention to further improve the efficiency of the algorithm.

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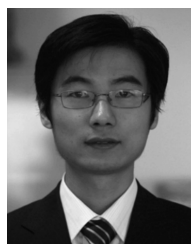
**Jiajun Wen** received the M.S. degree in applied computer technology from Guangdong University of Technology, Guangzhou, China, in 2010. He is currently working toward the Ph.D. degree in computer science and technology with Shenzhen Graduate School, Harbin Institute of Technology, Harbin, China.

He has been a Research Associate with Hong Kong Polytechnic University, Hong Kong, since 2013. His research interests include pattern recognition and video analysis.



**Yong Xu** (M'06) received the B.S. and M.S. degrees from the Air Force Institute of Meteorology, Nanjing, China, in 1994 and 1997, respectively, and the Ph.D. degree in pattern recognition and intelligence system from Nanjing University of Science and Technology, Nanjing, in 2005.

He was a Post-Doctoral Research Fellow with Shenzhen Graduate School, Harbin Institute of Technology, Harbin, China, from 2005 to 2007, where he is currently a Professor. He was a Research Assistant with Hong Kong Polytechnic University, Hong Kong, from 2007 to 2008. He has authored more than 60 scientific papers. His research interests include pattern recognition, biometrics, and machine learning.



**Jinhui Tang** (S'03–M'08) received the B.E. and Ph.D. degrees from University of Science and Technology of China, Hefei, China, in 2003 and 2008, respectively.

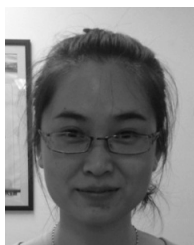
He was a Research Fellow with the School of Computing, National University of Singapore, Singapore, after graduation. He was a Research Intern with Microsoft Research Asia, Beijing, China, from 2006 and 2007, and a Visiting Research Scientist with the Department of Information and Computer Science, University of California at Irvine, Irvine, CA, USA, in 2010. In 2010 he joined the School of Computer Science and Technology, Nanjing University of Science and Technology, Nanjing, China, where he is currently a Professor. He has authored 60 journals and conference papers. His research interests include semantic-based image retrieval, social media analysis, and multimedia data management.

Dr. Tang is a member of the Association for Computing Machinery (ACM). He was a Guest Editor of *IEEE TRANSACTIONS ON MULTIMEDIA*, the *ACM Transactions on Intelligent Systems and Technology*, the *ACM/Springer's Multimedia System* journal, and the *Journal of Visual Communications and Image Representation*, *Neurocomputing*, and Springer's *Multimedia Tools and Applications* journal. He is the Co-Chair of the ACM First International Workshop on Web-Scale Multimedia Corpus in 2009, the Special Session Chair of the ACM Third International Conference on Internet Multimedia Computing and Service in 2011, a Technical Program Committee Member of over 30 international conferences, and a reviewer of over 30 prestigious international journals. He received the 2008 President Scholarship of the Chinese Academy of Science and the Excellent Doctoral Dissertation Award of Anhui Province, and was a co-recipient of the Best Paper Award at the 2007 ACM Multimedia Conference.



**Yinwei Zhan** (M'03) received the B.S., M.S., and Ph.D. degrees in mathematics from Jilin University, Changchun, China, in 1986 and 1988, respectively, and from Dalian University of Technology, Dalian, China, in 1992.

He was a Post-Doctoral Researcher with Beijing Normal University, Beijing, China, from 1992 to 1994 and an Associate Professor with Shantou University, Shantou, China, before becoming a Post-Doctoral Researcher at Centrum Wiskunde and Informatica, Amsterdam, The Netherlands, and Groningen University, Groningen, The Netherlands, from 2001 to 2004. Since 2005, he has been a Professor with the School of Computer, the Guangdong University of Technology, Guangzhou, China, where he is the Director of the Visual Information Processing Research and Development Center. His research interests include computer vision and pattern recognition.



**Xiaotang Guo** is working toward the M.S. degree in computer science and technology from Shenzhen Graduate School, Harbin Institute of Technology, Harbin, China.

Her research interests include pattern recognition and video analysis.



**Zhihui Lai** received the B.S. degree in mathematics from South China Normal University, Guangzhou, China, in 2002; the M.S. degree from Jinan University, Guangzhou, in 2007; and the Ph.D. degree in pattern recognition and intelligence system from Nanjing University of Science and Technology, Nanjing, China, in 2011.

He has been a Research Associate and a Post-Doctoral Fellow with Hong Kong Polytechnic University, Hong Kong, since 2010. He is currently a Post-Doctoral Fellow with the Bio-Computing Research Center, Shenzhen Graduate School, Harbin Institute of Technology, Harbin, China. His current research interests include face recognition and image processing.