Relaxed Asymmetric Deep Hashing Learning: Point-to-Angle Matching

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Abstract—Due to the powerful capability of the data representation, deep learning has achieved a remarkable performance in supervised hash function learning. However, most of the existing hashing methods focus on point-to-point matching that is too strict and unnecessary. In this article, we propose a novel deep supervised hashing method by relaxing the matching between each pair of instances to a point-to-angle way. Specifically, an inner product is introduced to asymmetrically measure the similarity and dissimilarity between the real-valued output and the binary code. Different from existing methods that strictly enforce each element in the real-valued output to be either +1 or −1, we only encourage the output to be close to its corresponding semantic-related binary code under the cross-angle. This asymmetric product not only projects both the real-valued output and the binary code into the same Hamming space but also relaxes the output with wider choices. To further exploit the semantic affinity, we propose a novel Hamming-distance-based triplet loss, efficiently making a ranking for the positive and negative pairs. An algorithm is then designed to alternatively achieve optimal deep features and binary codes. Experiments on four real-world data sets demonstrate the effectiveness and superiority of our approach to the state of the art.

Index Terms—Asymmetric, deep learning, hashing learning, point-to-angle, triplet loss.

I. INTRODUCTION

DUE to the rapid development of the internet, multimedia data in search engines and social networks meets a great increase in recent years. Subsequently, how to store these data and allow searches to have a quick query when a test sample is given has become a fundamental problem. Fortunately, hashing techniques provide a reasonable solution, thanks to its low storage cost (a few binary bits per sample) and fast retrieval speed (low complexity of the Hamming distance computation). The main goal of hashing methods is to learn multiple hash functions to project the input to a more compact Hamming space, in which the feature is represented as binary codes. Since these codes further enjoy the semantic or structure information existing in the original space, hashing methods have been used in many applications with a large-scale data set, e.g., image retrieval [1]–[3], pattern recognition [4]–[6], and data fusion [7].

Generally, hashing methods can be classified into two categories: data-independent and data-dependent. A typical data-independent method is the locality sensitive hashing (LSH) [8]. Although LSH is quite simple and easy to be implemented, it cannot meet our requirements when the length of the binary codes is relatively small due to the random hashing functions that are too weak to capture the complex distribution of the input data. To address this problem, data-dependent methods aim to learn adaptive hashing functions based on the input data, achieving much better performances with fewer binary bits per sample compared with LSH. Anchor graph hashing (AGH) [9] and spectral hashing (SH) [10] introduce the graph-based hashing methods to automatically discover the neighborhood structure inherent in the data to learn appropriate compact codes. However, these two methods discard the discrete constraints by solving the continuous problems. Therefore, discrete graph hashing (DGH) [11] further presents a tractable alternating maximization algorithm to deal with the discrete constraints. In addition, instead of using hyperplane-based hashing functions, spherical hashing [12] proposes a novel hypersphere-based hashing function, being capable of mapping more spatially coherent data points into a binary code. Despite the fact that the aforementioned methods learn the data-driven based hashing functions, the supervised information that is valuable for the performance improvement...
2) The asymmetric inner product end structure. For instance, deep pairwise supervised hashing jointly train the features and hashing functions in an end-to-large-scale data sets, which have complex distributions. Fortunately, traditional data-dependent hashing methods are superior to codes and preserve the label-based similarity. Although these simultaneously project the original features to compact binary (FastH) [13] and supervised discrete hashing (SDH) [14] is ignored. To tackle this problem, fast supervised hashing (FastH) [13] and supervised discrete hashing (SDH) [14] simultaneously project the original features to compact binary codes and preserve the label-based similarity. Although these methods are superior to codes and preserve the label-based similarity. Although these methods are superior to codes and preserve the label-based similarity.

Fig. 1. Motivation of the point-to-angle matching. Assume \( f_1, f_2, f_3, f_4, f_5, f_6, b_1, b_2 \) belong to the same Hamming space \( R_1 \). 1) \((f_1 f_2 - k)^2\) makes them similar and discrete. However, if \( f_1 \) and \( f_2 \) are both transformed to \( f'_1 \) and \( f'_2 \) in \( R_2 \), the value of \( f'_1 f'_2 \) remains unchanged but their hashing codes change.

2) The asymmetric inner product \((f_1 f_2 - k)^2\) can well tackle the problem in 1), but this term strongly enforces each element in \( f_1 \) (\( f_2 \)) to approximate to be either +1 or −1. This is too strict and unnecessary since what we need is sign\((f_1)\). 3) To address the problem in 2), although some works try to use the cosine distance to measure the similarity, it may be unable to process some specific cases like \((f_5, f_4)\).

This problem, several studies [19] try to use the asymmetric loss \((f_1 f_2 b_1 - kS_{1j})^2\) to alternatively update binary code \( b_1 \) and real-valued output \( f_2 \). Experimental results demonstrate the superiority of this asymmetric inner product. Note that what we require are the binary codes sign\((f_1)\) and sign\((f_2)\). Thus, encouraging \( f_1, f_2, b_1 \) to be in the same Hamming space is necessary, while the traditional asymmetric product \((f_1 f_2 b_1)\) not only enforces \( f_1 \) (\( f_2 \)) and \( b_1 \) in the same Hamming space but also requires them to be close in Euclidean distance, which is too strict and unnecessary. Therefore, Cao et al. [20] and He et al. [21] introduced the cosine distance \((\langle f_1, f_2 \rangle / \|f_1\|\|f_2\|)\) to make similar points lie in the same hypercube with high probability. However, this method also cannot meet our requirement in some specific cases. As shown in Fig. 1, assume \((f_1, f_4)\) and \((f_5, f_6)\) enjoy the same semantic information. We favor \( f_3 \) and \( f_6 \), but avoid \( f_3 \) and \( f_4 \). In fact, the cosine distance in both pairs is large, while \( f_3 \) and \( f_4 \) have different hashing codes. Therefore, based on the aforementioned analysis, we propose a novel relaxed asymmetric strategy to achieve the matching through point-by-angle. Particularly, as shown in Fig. 1, points \( f_3 \) and \( f_6 \) are encouraged to be close to the binary variable \( b_1 \) in cosine distance. Thanks to this strategy, we can not only make samples belonging to the same class in a common hypercube without any length constraint but also efficiently avoid the case occurring between \( f_3 \) and \( f_4 \).

The second problem is how to efficiently exploit the semantic affinity existing in the original space. In recent years, several functions have been proposed to reveal the similarity and dissimilarity between each pair of samples. The two commonest ways are the pairwise loss and triplet loss. The pairwise loss enforces the samples belonging to the same class to be close while those belonging to different classes to be far. In contrast, the triplet loss encourages the distance between each pair of similar (positive) samples to be smaller than that between each pair of dissimilar (negative) samples. In fact, in the image retrieval task, what we need is to make the similar samples closer than other dissimilar samples. Thus, we focus on using the triplet loss to measure the semantic affinity.

In fact, in the image retrieval task, what we need is to make the similar samples closer than other dissimilar samples. Thus, we focus on using the triplet loss to measure the semantic affinity. The traditional triplet loss uses the Euclidean distance to separate the similar and dissimilar pairs. However, the Euclidean distance is not adaptive for our relaxed asymmetric method. As shown in Fig. 2, \( f_1 \) and \( f_2 \) belong to the same category and are located in the same Hamming space, while \( f_3 \) is dissimilar to them and falls in another Hamming space. In fact, both \( f_1 \) and \( f_2 \) are in appropriate positions in the relaxed point-to-angle viewpoint since their cosine distances to \( b_1 \) are large. However, the Euclidean distance between \( f_1 \) and \( f_2 \) is much larger than that between \( f_2 \) and \( f_3 \). Therefore, if the traditional triplet loss is directly used for semantic information exploration, there would be an influence on our proposed relaxed asymmetric strategy. To address this problem, we propose a novel triplet loss based on the Hamming distance. Particularly, we first normalize the output onto a relaxation variable \( \Phi \) and then compute the following term:
multidimensional unit ball and get \( f_1, f_2 \) and \( f_3 \) corresponding to \( f_1, f_2 \) and \( f_3 \), respectively. Different from traditional methods that only consider the Euclidean distance in the triplet loss, we further use the Hamming distance to encourage \( f_1, f_2, \) and \( f_3 \) to be closer than \( f_1 \) to \( f_2 \) and \( f_3 \) under the Hamming distance.

The main contributions are concluded as follows.

1) A relaxed asymmetric strategy is proposed to reveal the similarity between real-valued outputs and discrete binary codes in point-to-angle matching. The real-valued features and hashing variables are encouraged to fall in the same Hamming space through an inner product without any length constraint.

2) A novel triplet loss is presented, which is quite adaptive for our proposed relaxed asymmetric method. Different from the traditional version that only ranks the positive and negative pairs by using the Euclidean distance, we normalize each output onto a multidimensional unit ball and the Hamming distance is introduced to make a ranking for different pairs.

3) An efficient algorithm is designed to alternatively update various variables in an end-to-end deep structure. Particularly, the binary codes can be obtained in a discrete way.

4) In image retrieval, experimental results on four large-scale data sets substantiate the effectiveness and superiority of our proposed method compared with some existing state-of-the-art hashing approaches.

The rest of this article is organized as follows. The related works, including both data-independent and data-dependent hashing methods, are briefly reviewed in Section II. In Section III, the proposed relaxed asymmetric deep hashing (RADH) is analyzed, followed by its optimization, inference, and implementation. In Section IV, experiments are conducted on four large-scale data sets to demonstrate the superiority of RADH. This article is finally concluded in Section V.

II. Related Works

As described in the first section, the hashing methods can be roughly divided into data-independent and data-dependent approaches.

LSH [8] is one of the most typical data-independent methods, which aims to use several randomly projections to get the hashing codes, ensuring the probability of collision is much higher for data points that are closer to each other than for those that are far apart. LSH is further extended to a kernel version (KLSH) [22] to nonlinearly represent the real-world data sets with more complex structures. In addition, various distance or similarity priors are also imposed on the basic LSH to achieve several extensions [23]–[25]. However, there is a performance limitation for LSH due to the fact that it is totally data-independent and ignores the data distribution that is valuable for the performance improvement.

To tackle this problem, researchers focus on the data-dependent methods to learn an adaptive hashing function for a specific data set. Generally, data-dependent methods can also be separated into two parts: unsupervised and supervised. Unsupervised hashing methods aim to exploit the structure information to learn compact codes for the input data. Density-sensitive hashing (DSH) [26] was proposed to replace the random projection in LSH. SH was proposed by Weiss et al. [10]. SH bridges the binary coding to the graph partitioning. Due to the high complexity of SH when the data set is large, Heo et al. proposed spherical hashing based on the hyperplane to learn a spherical Hamming distance [12]. Jiang and Li [27] proposed a scalable graph hashing (SGH) for large-scale graph hashing. Different from SH and SGH that ignore the discrete constraint, the DGH [11] was studied, which can find the inherent neighborhood structure in a discrete code space. In contrast to graph hashing, iterative quantization (ITQ) [28] and double-bit quantization (DBQ) [29] were presented to minimize the quantization error. Instead of measuring data similarity by the Euclidean distances, Hu et al. [30] designed a cosine similarity-based hashing learning strategy to achieve better performances. Different from unsupervised hashing methods that ignore the label information in the training set, supervised hashing learning focuses on learning the hash function to encourage the projected hashing codes to preserve the semantic information existing in the original space. Some typical supervised hashing approaches include kernel-based supervised hashing (KSH) [31], FastH [13], SDH [14], and column sample-based discrete supervised hashing (COSDISH) [32]. Both KSH and FastH achieve nonlinearity in supervised hashing, while SDH and COSDISH optimize their models discretely. Considering that there do exist potentially noisily labeled samples, the robust discrete code modeling (RDCM) [33] was presented to employ \( l_{2,p} \)-norm, being capable of performing code selection and noisy sample identification.

Although many data-dependent methods have been studied, they often meet a performance limitation due to the use of hand-crafted features. In recent years, deep learning with
an end-to-end network provides a reasonable and promising solution. A deep network was proposed by Liong et al. [34] to jointly represent the data and obtain binary codes. Due to the powerful image representation, convolutional neural networks (CNN) are widely applied to hashing learning. For instance, Zhang et al. [35] combined the CNN and hashing learning in a unified model and applied it to image retrieval and person re-identification. Similarly, deep hashing network (DHN) [36], deep supervised hashing (DSH-DL) [37], and CNN-based hashing (CNNH) [38] were also proposed. A pairwise loss (DPSH) was presented in [17] to preserve the semantic information between each pair of outputs. Shen et al. [39] deep asymmetric pairwise hashing (DAPH) and Jiang and Li asymmetric deep supervised hashing (ADSH) [19] proposed asymmetric structures and experimental results demonstrated their superiority. Note that an asymmetric hashing method, named asymmetric inner-product binary coding (AIBC), was previously proposed in [40] by revealing the inner products between raw data vectors and the discrete vectors, whose objective function is similar to that of ADSH. However, our proposed method is greatly different from these three asymmetric methods. For ADSH and AIBC, they only try to use the point-to-point based inner product to link the relationship between the real-valued output and the discrete variable. By contrast, RADH transforms the point-to-point operation to the point-to-angle way, which can provide more freedom for the estimation of the real-valued outputs. This strategy is more adaptive and reasonable for hashing learning, being beneficial to the performance improvement. Referring to DAPH, it only takes two streams of networks for training, while the Hamming distance-based measurement between the binary variable and the real-valued output is ignored. By contrast, our proposed method RADH not only takes the two-stream network into account but also introduces a novel measurement between the binary variable and the real-valued output.

To exploit the ranking information, the triplet labels are used to learn hashing models, including deep semantic ranking-based hashing (DSRH) [41], deep similarity comparison hashing (DSCH) [35], deep regularized similarity comparison hashing (DRSCH) [35], and unsupervised deep triplet hashing (UDTH) [42]. Note that, although UDTH uses the cosine similarity to construct the pseudo, it still exploits the Euclidean distance to measure the similarity and dissimilarity. Since there is not any length constraint on the learned features in RADH, these existing triplet losses are unsuitable to be directly applied to RADH. By contrast, our proposed triplet loss not only normalizes each learned feature to a unit length first but also transforms the Euclidean distance to the relaxed Hamming distance, which is more suitable for hashing learning. In addition, Heo et al. [12], [43] proposed a hypersphere-based hashing method, in which the pivot positions of two hyperspheres are made closer if the number of data points in a subset corresponding to two hashing functions are smaller or equal to a threshold. Otherwise, the pivots would be placed farther away. By contrast, our proposed method exploits the relaxed Hamming distance to encourage the distance between the positive pair to be smaller than that between the negative pair, which introduces the ranking information, being quite different from the measurement in [12] and [43]. Also, Gordo et al. [44] proposed the asymmetric schemes to binarize the database signatures but not the query. Differently, our presented approach exploits the supervised information between the binary codes and real-valued features, as well as the positive pairs and negative pairs.

III. PROPOSED METHOD

In this section, we first define the deep structure and some notations used in this article. The presented RADH is then analyzed, followed by its optimization, inference, and implementation.

A. Network Structure and Notations

In [39], it has been proved that the asymmetric deep network can preserve more similarity information. Note that in this article, we mainly focus on the efficiency of the relaxed asymmetric and novel triplet losses. Thus, we only simply apply the CNN-F [45] and the asymmetric deep network [39].
to represent the input data, as shown in Fig. 3. The main advantage of this two-stream network is that we can regard the input in one stream as the query and view the other one as the database, which is beneficial for updating the weights in each stream in a supervised way. It is obvious that this deep structure can be replaced with other network structures, e.g., VGG and ResNet, whereas these different structures are not the focus of this article.

Since we prefer to obtain a k-bit binary code, the last layer in CNN-F is replaced with a k-D vector. Besides this, we initialize the weights of the first seven layers in CNN-F by using the pretrained ImageNet model, where the weights in the last layer are set to be random values. Here we denote the inputs in the first and second streams as \( X = \{x_1, \ldots, x_d, \ldots, x_N\} \in \mathbb{R}^{N \times d_1 \times d_2 \times 3} \) and \( Y = \{y_1, \ldots, y_i, \ldots, y_N\} \in \mathbb{R}^{N \times d_1 \times d_2 \times 3} \), where \( N \) is the number of training samples and \((d_1, d_2)\) are the size of an image. Note that \( X \) and \( Y \) are only different in symbol notations. They both represent the same training set. Being similar to [39], the purpose of our model is to learn two hash functions \( F \) and \( G \) to map the raw data \( X \) and \( Y \) into the Hamming space. In this article, we denote the outputs associated with \( X \) and \( Y \) as \( F = [f_1, \ldots, f_i, \ldots, f_N]^T \in \mathbb{R}^{N \times k} \) and \( G = [g_1, \ldots, g_i, \ldots, g_N]^T \in \mathbb{R}^{N \times k} \), respectively. In addition, their corresponding shared binary codes are denoted as \( B = [b_1, b_i, \ldots, b_N]^T \in \mathbb{R}^{N \times k} \), where \( b_i \in \{-1, +1\}^k \) as our method performs supervised learning, a matrix \( S \in \mathbb{R}^{N \times N} \) is introduced to measure the semantic similarity between \( X \), \( Y \), and \( B \). \( S_{ij} \) is its element in the \( i \)th row and \( j \)th column. \( S_{ij} = 1 \) if \( x_i \) and \( y_j \) share the same semantic information or label, otherwise \( S_{ij} = 0 - \epsilon \), where \( \epsilon \) is a slack variable, e.g., 0.11. Note that, the sizes of \( F, G \), and \( B \) are all the same. In our two-stream network, being the same to DAPH, we input the images \( X \) and \( Y \) (both are the same training set) into the first and second streams alternatively. When the images are inputted into the first stream and get the output \( F \), we encourage \( F \) to do retrieval from \( G \). The second stream carries out the same operation. Then \( B \) is the binary code that is completely associated with \( F \) and \( G \) row by row.

### B. RADH

The framework of the proposed method is shown in Fig. 3. There are two streams and both are used to extract the features from the input images. Different from DAPH [39] that learns two binary codes associated with these two streams, we aim to learn a shared hashing code associated with the outputs from the first and second streams. More specifically, a relaxed asymmetric strategy is used to encourage the real-valued outputs and the discrete hashing variables enjoying the same semantic information to be close in terms of the cosine distance. The novel triplet loss is then introduced to make an efficient ranking for each positive and negative pair.

Let \( F \) and \( G \) be the outputs in the first and second streams, respectively. Since our goal is to obtain hash functions through the deep networks, the binary code \( B \) is also generated by minimizing the distance between \( B \) and \( F / G \). As analyzed in DAPH and ADSH, the asymmetric strategy can reduce the difficulty of the discrete constraint optimization. Equation (1) is used to not only make the real-valued outputs and the hashing variables close in Hamming distance but also enjoy the semantic affinity existing in the original space

\[
\min \left( \frac{b_i^T f_j - k S_{ij}}{2} + \frac{b_i^T g_j - k S_{ij}}{2} \right)
\]

However, (1) also enforces \( F \) or \( G \) to be similar in the length, which is too strict and unnecessary. What we need is to ensure the hashing codes and real-valued outputs to have the same semantic information in a common Hamming space rather than the same length. To address this problem, we relax (1) to (2).

\[
\min \left( \left( \frac{b_i^T f_j}{\|b_i\| \|f_j\|} - S_{ij} \right)^2 + \left( \frac{b_i^T g_j}{\|b_i\| \|g_j\|} - S_{ij} \right)^2 \right)
\]

where \( \|b_i\|, \|f_j\|, \) and \( \|g_j\| \) represent the length of \( b_i, f_j \), and \( g_j \), respectively. Since \( \|b_i\| = \sqrt{k} \), we further transform (2) to (3).

\[
\min L_a = \sum_{i,j} \left( \left( \frac{b_i^T f_j}{\|f_j\|} - \sqrt{k} S_{ij} \right)^2 + \left( \frac{b_i^T g_j}{\|g_j\|} - \sqrt{k} S_{ij} \right)^2 \right)
\]

From (3), it is easy to see that there is not any length constraint on the learned features, while this equation simultaneously makes the real-valued outputs and binary codes locate in the same hypercube if they belong to the same class, otherwise they will be located in different Hamming spaces. Compared with (1), this strategy provides more freedom for the estimation of \( f_j \) and \( g_j \), which is more adaptive and reasonable for hashing learning.

In the retrieval task, what we need is to ensure the distance between each positive pair to be smaller than that of the corresponding negative pair. Thus, we further introduce the triplet loss, which is quite adaptive for the retrieval task. However, directly applying the existing triplet loss to RADH is not reasonable due to the following two limitations.

1) In hashing learning, the input vectors for the existing triplet loss often follow the constraint that each element is encouraged to be \(+1\) or \(-1\), so that their lengths would be limited to a narrow range. However, there is not any length constraint on the vectors in RADH, which makes the existing triplet loss unsuitable for our proposed method, as shown in Fig. 2.

2) The adaptive measurement in hashing learning is the Hamming distance, while the existing triplet loss often adopts the Euclidean distance to measure the similarity or dissimilarity, subsequently resulting in the quantative error.

By contrast, in this article, we propose a novel triplet loss that is quite suitable for RADH. Particularly, we first normalize the real-valued features to a unit ball so that the vector length problem can be well avoided. The inner product of two outputting vectors is then introduced as the relaxed Hamming distance, which would be more adaptive and reasonable for our hashing learning.

Our proposed triplet comparison formulation is trained on a series of triplets \((f_i, f_j, f_{i'})\), where \( f_i \) and \( f_j \) belong to the same class, while \( f_j \) and \( f_{i'} \) are from different classes. The
same formulation can be applied to \((g_i, g_j, g_k)\). To make the Hamming distance between \(f_i\) and \(f_j\), smaller than that between \(f_i\) and \(f_k\), for any triplet \((f_i, f_j, f_k)\), these three samples should satisfy the following constraining:

\[
\left( \frac{t_i^T f_j}{\|f_i\| \|f_j\|} - 1 \right)^2 - \left( \frac{t_i^T f_k}{\|f_i\| \|f_k\|} - 1 \right)^2 > 1 - \xi_{ij} \tag{4}
\]

where \(\xi_{ij}\) is a nonnegative slack variable. Note that since there is no particular constraint on the length of the output, we first normalize \((f_i, f_j, f_k)\) onto a \(k\)-dimensional unit ball. However, it is difficult to get the gradient of \(f_j\) since it may also be associated with other samples as a retrieval point. Thanks to our two-stream network structure, we can regard \(f_j\) as a query, while \(\{g_i\}_{i=1}^N\) is used as a retrieval data set. Thus, jointly taking \((f_i, f_j, f_k)\) and \((g_i, g_j, g_k)\) into account, the triplet loss function in RADH is

\[
\min L_p = \sum_{i,j,l} \left[ 1 - \left( \frac{g_i^T f_j}{\|g_i\| \|f_j\|} - 1 \right)^2 + \left( \frac{g_i^T f_l}{\|g_i\| \|f_l\|} - 1 \right)^2 \right] + \\
+ \sum_{i,j,l} \left[ 1 - \left( \frac{t_i^T g_j}{\|t_i\| \|g_j\|} - 1 \right)^2 + \left( \frac{t_i^T g_l}{\|t_i\| \|g_l\|} - 1 \right)^2 \right] \tag{5}
\]

where \([z]_+ = \max(z, 0)\). Compared with the existing triplet loss that only uses the Euclidean distance to measure the ranking between the positive and negative pairs, (5) successfully transforms it to a hashing-based function, efficiently exploiting the Hamming distance to achieve a satisfactory ranking.

As described in [39], an additional Euclidean regularization between \(b_j\) and \(f_j\) / \(g_j\) is beneficial to the performance improvement. Thus, we further enforce \(b_j\) and \(f_j\) / \(g_j\) to be close in terms of the Euclidean distance as shown in the following equation:

\[
\min L_e = \sum_j \left[ \left( \sqrt{k} f_j \|f_j\| - b_j \right)^2 + \left( \sqrt{k} g_j \|g_j\| - b_j \right)^2 \right] \tag{6}
\]

Here \(\sqrt{k} f\) / \(\|f\|\) and \(\sqrt{k} g\) / \(\|g\|\) are applied to make their elements close to either \(-1\) or \(+1\).

In addition, as shown in (7), in order to achieve a balance for each bit in the training samples, as well as to maximize the information provided by each bit, another regularization is introduced

\[
\min L_r = \|\sqrt{k} F^T 1\|_2^2 + \|\sqrt{k} G^T 1\|_2^2 \tag{7}
\]

where \(\bar{F} = [\bar{f}_1, \ldots, \bar{f}_N]^T = [(t_i/\|t_i\|), \ldots, (t_N/\|t_N\|)]^T\), \(\bar{G} = [\bar{g}_1, \ldots, \bar{g}_N]^T = [(g_i/\|g_i\|), \ldots, (g_N/\|g_N\|)]^T\) and \(1\) is a \(N \times 1\) vector whose elements are all 1.

Overall, the objective function can be obtained as follows:

\[
\min L_a + \tau L_p + \gamma L_e + \eta L_r, \quad \text{s.t. } b_i \in \{-1, +1\} \tag{8}
\]

where \(\tau, \gamma, \) and \(\eta\) are the nonnegative parameters to make a tradeoff among various terms.

### C. Optimization

In the objective function (8), the variables including \(F\), \(G\) and \(B\) should be optimized. Due to the discrete constraint on \(B\), it is difficult to get the optimal solution directly. In this article, an efficient algorithm is designed to alternately and discretely update different variables.

1) Update \(F\) With \(G\) and \(B\) Fixed: By fixing \(G\) and \(B\), the objective function (8) is transformed to

\[
\min L_f = \sum_{i,j} \left( b_i^T (\bar{f}_j - \sqrt{k} S_{ij})^2 + \gamma \sum_j \|\sqrt{k} \bar{f}_j - b_j \|_2^2 \right) \times \tau \sum_{i,j} \left[ 1 - (g_i^T \bar{f}_j - 1)^2 + (g_i^T \bar{f}_j - 1)^2 \right]_+ \\
+ \eta \|\sqrt{k} F^T 1\|_2^2 \tag{9}
\]

We obtain the following derivative of \(L_f\) with respect to \(\bar{f}_j\):

\[
\frac{\partial L_f}{\partial \bar{f}_j} = 2 \sum_i b_i (b_i^T (\bar{f}_j - \sqrt{k} S_{ij}) - 2 \sqrt{k} (\sqrt{k} \bar{f}_j - b_j)) \\
+ 2 \tau \sum_{i,j} M_{ij} (-g_i (g_i^T \bar{f}_j - 1) + g_i (g_i^T \bar{f}_j - 1)) \\
+ 2 \eta \sqrt{k} F^T 1 \tag{10}
\]

where \(M\) is a mask matrix and its component in the \(i\)th row and \(j\)th column is denoted as \(M_{ij}\), \(M_{ii} = 1\) if \(1 - (\bar{f}_i^T \bar{f}_j - 1)^2 + (\bar{f}_i^T \bar{f}_j - 1)^2 > 0\), otherwise \(M_{ii} = 0\).

Then the derivative of \(\bar{f}_j\) with respect to \(b_j\) is calculated as follows:

\[
\frac{\partial \bar{f}_j}{\partial b_j} = \frac{1}{\|\bar{f}_j\|} - \frac{\bar{f}_j \bar{f}_j^T}{\|\bar{f}_j\|^3} \tag{11}
\]

Combining (10) and (11) together and exploiting the chain rule, the derivative of \(L_f\) with respect to \(\bar{f}_j\) is

\[
\frac{\partial L_f}{\partial \bar{f}_j} = \frac{\partial \bar{f}_j}{\partial b_j} \frac{\partial L_f}{\partial b_j} \tag{12}
\]

After getting the gradient \(\frac{\partial L_f}{\partial \bar{f}_j}\), the chain rule is used to obtain \(\frac{\partial L_f}{\partial W_f}\), where \(W_f\) is the weight in the first stream, \(W_f\) is updated by using backpropagation.

2) Update \(G\) With \(F\) and \(B\) Fixed: By fixing \(F\) and \(B\), the objective function (8) is transformed to

\[
\min L_g = \sum_{i,j} \left( b_i^T (\bar{g}_j - \sqrt{k} S_{ij})^2 + \gamma \sum_j \|\sqrt{k} \bar{g}_j - b_j \|_2^2 \right) \times \tau \sum_{i,j} \left[ 1 - (\bar{f}_i^T \bar{g}_j - 1)^2 + (\bar{f}_i^T \bar{g}_j - 1)^2 \right]_+ \\
+ \eta \|\sqrt{k} G^T 1\|_2^2 \tag{13}
\]

Similarly, the derivative of \(L_g\) with respect to \(g_j\) is

\[
\frac{\partial L_g}{\partial g_j} = \frac{\partial \bar{g}_j}{\partial g_j} \frac{\partial L_g}{\partial \bar{g}_j} \tag{14}
\]
where

\[
\frac{\partial \hat{g}_j}{\partial g_j} = \frac{1}{\|g_j\|} - \frac{g_j g_j^T}{\|g_j\|^2},
\]

\[
\frac{\partial L_g}{\partial g_j} = 2 \sum_i b_i (f_i^T g_j - \sqrt{k}S_{ij}) + 2\gamma \sqrt{k} (\sqrt{k}g_j - b_j) + 2\tau \sum_{i,t} M_{it} (-\hat{r}_i (f_i^T g_j - 1) + \hat{r}_i (f_i^T g_j - 1)) + 2\eta k \hat{G}_j^T 1.
\]

After getting the gradient \(\frac{\partial L_g}{\partial g_j}\), we use the chain rule to obtain \(\frac{\partial L_g}{\partial W_g}\), where \(W_g\) is the weight in the second stream. \(W_g\) is updated by using backpropagation.

3) Update \(B\) With \(F\) and \(G\) Fixed: By fixing \(F\) and \(G\), the objective function (8) is transformed to

\[
\min L_b = \|FB^T - \sqrt{k}S||_F^2 + \|GB^T - \sqrt{k}S||_F^2 + \gamma (\|\sqrt{k}F - B||_F^2 + \|\sqrt{k}G - B||_F^2)
\]

s.t. \(b_i \in \{-1, +1\}\).

Then (17) can be rewritten as

\[
\min L_b = -2 \text{Tr} \left( B \left( \sqrt{k}(FF^T + GG^T) (S + \gamma I) \right) \right) + \|BF^T||_F^2 + \|BG^T||_F^2 + \text{const.}
\]

s.t. \(b_i \in \{-1, +1\}\).

Since it is difficult to optimize \(B\) directly, we update it bit by bit. In other words, we update one column in \(B\) with remaining columns fixed. Denote \(B_{sc}\) as the \(c\)th column and \(B_c\) as the remaining columns in \(B\). The same can be applied to \(F_{sc}, F_c, G_{sc}, G_c, Q_{sc},\) and \(Q_c\). When we optimize \(B_{sc}\), (19) can then be rewritten as

\[
\min B_{sc} \text{Tr} \left( B_{sc} \left[ 2(F_{sc}F_c + G_{sc}G_c)B_c^T + Q_{sc} \right] \right) + \text{const.}
\]

s.t. \(B \in \{-1, +1\}^{n \times k}\).

It is easy to get the optimal solution for \(B_{sc}\)

\[
B_{sc} = -\text{sign}(2\hat{B}_c (F_{sc}^T F_c + G_{sc}^T G_c) + Q_{sc}).
\]

After computing \(B_{sc}\), we update \(B\) by replacing the \(c\)th column with \(B_{sc}\). Then we repeat (21) until all columns are updated. Algorithm 1 shows the details of the optimization.

**Algorithm 1 RADH**

**Input:** Training data \(X/Y\); similarity matrix \(S\); hash code length \(k\); predefined parameters \(\tau, \gamma\), and \(\eta\).

**Output:** Hashing functions \(F\) and \(G\) for the two streams, respectively.

**Initialization:** Initialize weights of the first seven layers by using the pretrained ImageNet model; the last layer is initialized randomly; \(B\) is set to be a matrix whose elements are zero.

1: while not converged or the maximum iteration is not reached do

2: \textbf{Update} \((F, W_f)\):

\(\text{Fix} (G, W_g)\) and \(B\) and update \((F, W_f)\) using back-propagation according to Eq.(12).

3: \textbf{Update} \((G, W_g)\):

\(\text{Fix} (F, W_f)\) and \(B\) and update \((G, W_g)\) using back-propagation according to Eq.(14).

4: \textbf{Update} \(B\):

\(\text{Fix} (F, W_f)\) and \((G, W_g)\) and update \(B\) according to Eq.(21).

5: end while

Their average as the final result, as shown in the following equation:

\[
b^* = \text{sign}(F(x^*, W_f) + G(x^*, W_g)).
\]

**E. Implementation**

We implement RADH under the deep learning toolbox MatConvNet [46] on a Titan X GPU. Specifically, the pretrained model of CNN-F on the ImageNet data set is applied to both streams to initialize their weights, which is greatly beneficial to the performance improvement. Since the output of the last layer is different from that in the original CNN-F model, we randomly initialize the weight in this layer. In the training phase, we set the maximized epoch to be 150, the learning rate to be \(10^{-3}\), the batch size to be 64, and the weight decay to be \(5 \times 10^{-4}\). The stochastic gradient descent (SGD) is then exploited to update the weights.

In (5), the triplet loss is achieved by ranking each positive pair and negative pair. However, it is too time consuming if we take all training samples into account. In our experiments, we sort the positive pairs in descending order and the negative pairs in ascending order by following \((f_i^T g_j - 1)^2 / (g_i^T f_j - 1)^2\). We then select top 200 samples from each part as the positive and negative instances, respectively.

**IV. EXPERIMENTS**

In this section, different experiments on four data sets are conducted based on different experimental settings. We first followed the settings in some existing methods to make a comparison between RADH and other deep hashing methods. In order to better demonstrate the generality of the proposed model, additional experiments based on our settings are also conducted, followed by the analysis on the sensitivity of the parameters \(\tau, \gamma\), and \(\eta\).
A. Data Sets and Evaluation Protocol

In this article, four real-world data sets, including CIFAR-10 [47], NUS-WIDE [48], IAPR-12 [49], and MIRFLICKR-25K [50], are used to evaluate the superiority of RADH.

**CIFAR-10** is composed of 60000 images, where each sample belongs to one of ten classes.

**NUS-WIDE** consists of 269648 web images. Following [17] and [19], 195834 images are selected, which are associated with the 21 most frequent tags. Since images in this data set are multilabel, $S_{ij} = 1$ if there is at least one label between $x_i$ and $x_j$, otherwise $S_{ij} = 0 - \varepsilon$. Here $\varepsilon$ is set to 0.11.

**IAPR-12** is composed of 20000 images associated with 255 classes. Note that some samples in the IAPR-12 data set have multiple labels. The definition of $S_{ij}$ is the same to that in NUS-WIDE.

**MIRFLICKR-25K** is composed of 25000 images collected from Flickr. Being similar to the IAPR-12 data set, this is also a multilabel data set. Here, we also define two images to be ground-truth neighbors if they share at least one common label. According to [51], 20015 images annotated with at least 24 tags are selected.

To quantitatively evaluate different approaches, the mean average precision (MAP) and top-k precision are adopted.

B. Existing Experimental Settings

Since the CIFAR-10 and NUS-WIDE data sets are the most common data sets used in existing deep hashing methods, we show the results conducted on these two data sets. Being similar to existing methods, MAP and Top-50000 MAP are applied to evaluate the performance of different approaches on the CIFAR-10 and NUS-WIDE data sets, respectively. Note that all results of the comparison methods in this subsection are directly copied from the published articles [17], [19], [35]. Besides, DRSCH, DSCH, and DSRH are the triplet label-based methods.

Note that, since the training number is quite large and if we use all training samples in each epoch, the required storage of the similarity matrix $S$ would be very huge, being impractical in the implementation. Thus, being similar to ADSH, we also randomly sample a part of instances from the training set in each epoch. Table I makes a comparison among RADH, DSH-DL, DHN, and ADSH conducted on the CIFAR-10 and NUS-WIDE data sets. Here 1000 samples are selected for testing (100 per class) and remaining samples are used for training in the CIFAR-10 and NUS-WIDE data sets. Since LSH, SpH, ITQ, and DSH are traditional

C. Additional Experimental Settings

Although our method obtains satisfactory performance in Table I, it cannot comprehensively show the generality of the models due to the too large number of training samples. To address this problem, we aim to divide the data set into three parts: training, retrieval, and testing sets.

**CIFAR-10**: 100 samples per class are used for testing, 500 samples per class are selected for training, and the remaining images are used for retrieval.

**NUS-WIDE**: 2100 images are selected for testing and the remaining images are used for retrieval, in which 10500 images are selected for training.

**IAPR-12**: The retrieval set consists of 18000 images and the test set is composed of the remaining 2000 images. Furthermore, we randomly select 5000 images from the retrieval set to be the training set.

**MIRFLICKR-25K** 2000 are used for testing while the remaining samples are regarded as the retrieval subset. Also, 5000 images from this retrieval subset are randomly selected for training.

Some existing hashing methods including data-independent and data-dependent are compared with our proposed method to demonstrate its superiority. These are LSH [8], SpH [12], ITQ [28], DSH [26], DPSH [17], ADSH [19], and DAPH [39]. Since LSH, SpH, ITQ, and DSH are traditional...
TABLE III
MAP@Top500 and Precision@Top500 Scores Obtained by Different Methods on the CIFAR-10 Data Set

<table>
<thead>
<tr>
<th>Evaluation Method</th>
<th>8-bit</th>
<th>12-bit</th>
<th>16-bit</th>
<th>24-bit</th>
<th>36-bit</th>
<th>48-bit</th>
</tr>
</thead>
<tbody>
<tr>
<td>LSH</td>
<td>17.73</td>
<td>24.97</td>
<td>29.06</td>
<td>28.03</td>
<td>30.39</td>
<td>32.59</td>
</tr>
<tr>
<td>SpH</td>
<td>31.10</td>
<td>32.87</td>
<td>33.41</td>
<td>38.64</td>
<td>41.24</td>
<td>43.35</td>
</tr>
<tr>
<td>ITQ</td>
<td>26.43</td>
<td>37.48</td>
<td>37.42</td>
<td>41.06</td>
<td>45.37</td>
<td>46.16</td>
</tr>
<tr>
<td>DSH</td>
<td>27.25</td>
<td>34.14</td>
<td>34.64</td>
<td>37.00</td>
<td>40.02</td>
<td>41.33</td>
</tr>
<tr>
<td>DPSH</td>
<td>58.58</td>
<td>66.85</td>
<td>71.48</td>
<td>75.74</td>
<td>79.69</td>
<td>80.62</td>
</tr>
<tr>
<td>ADSH</td>
<td>58.92</td>
<td>70.07</td>
<td>74.95</td>
<td>78.09</td>
<td>78.85</td>
<td>77.61</td>
</tr>
<tr>
<td>DAPH</td>
<td>50.88</td>
<td>66.24</td>
<td>72.43</td>
<td>77.31</td>
<td>79.21</td>
<td>80.40</td>
</tr>
<tr>
<td>RADH</td>
<td>68.72</td>
<td>70.39</td>
<td>77.36</td>
<td>79.39</td>
<td>82.90</td>
<td>84.92</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Method</th>
<th>8-bit</th>
<th>12-bit</th>
<th>16-bit</th>
<th>24-bit</th>
<th>36-bit</th>
<th>48-bit</th>
</tr>
</thead>
<tbody>
<tr>
<td>LSH</td>
<td>14.37</td>
<td>18.30</td>
<td>22.85</td>
<td>22.70</td>
<td>25.54</td>
<td>27.19</td>
</tr>
<tr>
<td>SpH</td>
<td>24.15</td>
<td>27.59</td>
<td>28.59</td>
<td>34.24</td>
<td>36.60</td>
<td>38.73</td>
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<td>ITQ</td>
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<td>40.78</td>
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<tr>
<td>DSH</td>
<td>24.47</td>
<td>28.20</td>
<td>29.33</td>
<td>33.07</td>
<td>35.54</td>
<td>36.55</td>
</tr>
<tr>
<td>DPSH</td>
<td>64.13</td>
<td>70.80</td>
<td>74.71</td>
<td>78.34</td>
<td>80.59</td>
<td>81.55</td>
</tr>
<tr>
<td>ADSH</td>
<td>61.09</td>
<td>73.71</td>
<td>78.85</td>
<td>81.84</td>
<td>83.45</td>
<td>82.86</td>
</tr>
<tr>
<td>DAPH</td>
<td>54.22</td>
<td>68.28</td>
<td>74.42</td>
<td>77.36</td>
<td>78.80</td>
<td>79.55</td>
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<tr>
<td>RADH</td>
<td>76.37</td>
<td>76.94</td>
<td>81.62</td>
<td>82.88</td>
<td>85.31</td>
<td>86.47</td>
</tr>
</tbody>
</table>

Fig. 4. PR curves computed by LSH, SpH, ITQ, SDH, SGH, DPSH, ADSH, DAPH, and RADH on the CIFAR-10 data set. (a)–(f) Figures associated with the code lengths of 8-bit, 12-bit, 16-bit, 24-bit, 36-bit, and 48-bit.

hashing methods, the features should be extracted in advance. In this article, we use the CNN feature to be the input for these methods. We implement RADH with the MatconvNet tool under the CNN-F structure. This is done to make a fair comparison since the released codes of DPSH and ADSH are also based on the MatconvNet and CNN-F. Also, since DAPH is similar to DPSH and can be easily re-implemented by using MatconvNet and CNN-F, we also make a comparison between RADH and DAPH. Specifically, for DPSH and ADSH that are all deep learning methods, we apply the CNN-F as the network for the feature extraction and parameters in them are set according to the descriptions in their publications. For DAPH, the original network is ResNet. We replace it with the CNN-F and try our best to tune the parameters in the modified DAPH. Specifically, these three deep hashing methods are implemented with MatConvNet and the raw image is their input. Note that DPSH, ADSH, and DAPH achieve the state-of-the-art performance in existing deep hashing methods. Thus, it is reasonable for us to only compare RADH with them.

Here the MAP is exploited as the evaluation protocol. Furthermore, being similar to [39], we also adopt the MAP of the top 500 retrieval samples (MAP@500) and the mean precision of the top 500 retrieval samples (Precision@500) as another two evaluation protocols.

1) Comparison With Other Methods: We make a comparison between the proposed method and other state-of-the-art approaches on four real-world data sets. Note that $\gamma$ and $\tau$ are set to 500 and 0.1 for the four data sets, respectively. $\eta$ is set to 0.3 for the NUS-WIDE, IAPR TC-12, and MIRFLICKR-25K data sets, while it is set to 1 for the CIFAR-10 data set. All these values are selected by cross-validation.

a) CIFAR-10: The experimental results about MAP scores obtained by different methods are tabulated in Table II. From this table, it is easy to see that RADH arrives to the highest points on the MAP score in all cases, especially when the code length is relatively small. Compared with LSH, SpH, ITQ, and DSH, which are not deep learning methods, DPSH, ADSH, DAPH, and our proposed RADH always get the better results. In contrast to these three deep comparison methods, RADH also has more or less improvement. Particularly, when the code length is only 8-bit, our method obtains the much larger enhancement, achieving more than 10% on the MAP score.

Table III further lists the MAP@Top500 and Precision@Top500 scores computed by different approaches. As we can see, RADH is still superior to other approaches. When the code length is set to be 8-bit, RADH achieves almost more than 10% enhancement on the both MAP@Top500 and Precision@Top500 scores, compared with all comparison methods. With the increase in the code length, although the performance gap meets a degradation, RADH is still superior to the other algorithms. Particularly, when the code length is set to be 48-bit, our proposed method gains about 4% improvement.

Fig. 4 plots the precision–recall (PR) curves when the code length ranges from 8-bit to 48-bit on the CIFAR-10 data set. It is obvious to observe that the presented strategy covers the largest or competitive areas. Except for the case when the
code length is 36-bit, RADH gains more or less improvement. In comparison to LSH, SpH, ITQ, and DSH, there are much larger areas computed by RADH. Although RADH only has a slight increase when the code length is 48-bit compared with DPSH, ADSH, and DAPH, it enlarges the gap of covered areas remarkably when the code length is 8-bit, 12-bit, 16-bit, and 24-bit, demonstrating its superiority.

b) NUS-WIDE: The MAP scores obtained by different methods are shown in Table IV. As we can see, the proposed method RADH achieves a remarkable improvement compared with other approaches. In contrast to the nondeep learning strategies, including LSH, SpH, ITQ, and DSH, RADH always gains about more than 15% enhancement. Referring to the deep hashing methods, RADH is still superior to them. Particularly, our presented approach obtains 73.47% on the MAP score, while the best performance computed by other deep hashing methods is only 68.12%.

Table V tabulates the MAP@Top500 and Precision@Top500 scores, which also demonstrate the superiority of the proposed method. Except for the case when the code length is 8-bit, RADH arrives to the highest points. In comparison to LSH, SpH, ITQ, and DSH, there is at least 5% improvement in both metrics. Compared with DPSH and DAPH, our approach still gains more or less enhancement. Note that, from Tables IV and V, we can see although ADSH obtains better results in the MAP score compared with ITQ, its MAP@Top500 and Precision@Top500 scores are much inferior to that of ITQ, relatively indicating its instability. By contrast, our proposed method RADH can get satisfactory results in MAP, MAP@Top500, and Precision@Top500 scores.

The PR curves computed by various methods are displayed in Fig. 5. It is easy to observe that RADH covers the largest areas when the code length ranges from 8-bit to 48-bit. Specifically, DPSH and RADH always gain satisfactory PR curves compared with other methods. In contrast to DPSH, RADH also achieves an obvious improvement.

c) IAPR TC-12: The experimental results on MAP scores obtained by various methods are listed in Table VI. As we can see, RADH gains better performance than all comparison methods. For instance, as listed in Table VI, the MAP scores computed by RADH are much higher than that obtained by LSH, SpH, ITQ, and DSH, which relatively demonstrate that data-independent and traditional data-dependent hashing methods are often inferior to deep hashing strategies. In contrast to other deep hashing methods, our proposed method is also superior. In most cases, RADH gets more than 4% improvement on the MAP score, indicating the effectiveness of our relaxed strategy and novel triplet loss.

Referring to MAP@Top500 and Precision@Top500 shown in Table VII, there is also a remarkable improvement for RADH compared with other approaches. In contrast to LSH, SpH, ITQ, and DSH, RADH gains more than 10% improvement on the MAP@Top500 and Precision@Top500 scores in most cases. In comparison to DPSH, ADSH, and DAPH, the proposed method also achieves more than 5% enhancement on the two evaluation protocols when the code length ranges from 12 to 48. Furthermore, in these three comparison deep hashing methods, although ADSH obtains better performance compared with DPSH and DAPH when the code length is 12, 16, 24, 36, or 48, it has much inferior results when the code
This article has been accepted for inclusion in a future issue of this journal. Content is final as presented, with the exception of pagination.

**TABLE VII**

<table>
<thead>
<tr>
<th>Evaluation</th>
<th>MAP@Top500</th>
<th>Precision@Top500</th>
</tr>
</thead>
<tbody>
<tr>
<td>Method</td>
<td>8-bit</td>
<td>12-bit</td>
</tr>
<tr>
<td>LSH</td>
<td>39.87</td>
<td>39.83</td>
</tr>
<tr>
<td>SpH</td>
<td>44.38</td>
<td>45.43</td>
</tr>
<tr>
<td>ITQ</td>
<td>51.75</td>
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<tr>
<td>DSH</td>
<td>48.34</td>
<td>48.63</td>
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<td>DPSH</td>
<td>57.07</td>
<td>58.13</td>
</tr>
<tr>
<td>ADSH</td>
<td>53.70</td>
<td>58.12</td>
</tr>
<tr>
<td>DAPH</td>
<td>56.26</td>
<td>57.98</td>
</tr>
<tr>
<td>RADH</td>
<td><strong>58.99</strong></td>
<td><strong>64.67</strong></td>
</tr>
</tbody>
</table>

**Fig. 6.** PR curves computed by LSH, SpH, ITQ, SDH, SGH, DPSH, ADSH, DAPH, and RADH on the IAPR TC-12 data set. (a)–(f) Figures associated with the code length of 8-bit, 12-bit, 16-bit, 24-bit, 36-bit, and 48-bit.

**TABLE VIII**

<table>
<thead>
<tr>
<th>Method</th>
<th>8-bit</th>
<th>12-bit</th>
<th>16-bit</th>
<th>24-bit</th>
<th>36-bit</th>
<th>48-bit</th>
</tr>
</thead>
<tbody>
<tr>
<td>LSH</td>
<td><strong>57.14</strong></td>
<td><strong>57.21</strong></td>
<td><strong>58.25</strong></td>
<td><strong>59.37</strong></td>
<td><strong>59.62</strong></td>
<td><strong>59.86</strong></td>
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<tr>
<td>SpH</td>
<td>59.20</td>
<td>60.71</td>
<td>60.91</td>
<td>60.97</td>
<td>61.63</td>
<td>62.43</td>
</tr>
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<td>ITQ</td>
<td>63.09</td>
<td>63.40</td>
<td>63.52</td>
<td>63.82</td>
<td>64.06</td>
<td>64.34</td>
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<td>DSH</td>
<td>64.48</td>
<td>63.83</td>
<td>64.10</td>
<td>65.96</td>
<td>65.90</td>
<td>65.62</td>
</tr>
<tr>
<td>DPSH</td>
<td>73.48</td>
<td>74.68</td>
<td>75.58</td>
<td>76.01</td>
<td>76.09</td>
<td>76.05</td>
</tr>
<tr>
<td>ADSH</td>
<td>75.39</td>
<td>76.41</td>
<td>76.98</td>
<td>76.59</td>
<td>76.20</td>
<td>74.53</td>
</tr>
<tr>
<td>DAPH</td>
<td>72.79</td>
<td>74.70</td>
<td>74.30</td>
<td>74.14</td>
<td>73.81</td>
<td>73.41</td>
</tr>
<tr>
<td>RADH</td>
<td><strong>75.50</strong></td>
<td><strong>76.77</strong></td>
<td><strong>78.09</strong></td>
<td><strong>79.18</strong></td>
<td><strong>80.13</strong></td>
<td><strong>80.38</strong></td>
</tr>
</tbody>
</table>

length is 8. By contrast, our proposed method RADH always gets the best performance no matter how long the code length is, relatively indicating its superiority.

Fig. 6 shows the PR curves obtained by different methods when the bit length ranges from 8 to 48. It is easy to observe that PR curves computed by RADH cover larger areas compared with that obtained by different comparison approaches. In comparison to DPSH, ADSH, and DAPH, RADH can get an obvious improvement due to the relaxed asymmetric strategy and the novel triplet loss.

d) MIRFLICKR-25K: The experimental results about MAP scores on the MIRFLICKR-25K data set computed by RADH and other comparison methods are tabulated in Table VIII. Similarly, our presented strategy is superior to other methods on this evaluation protocol. Making a comparison between the deep learning-based hashing methods and data-independent and traditional data-dependent approaches, deep hashing methods achieve much better results. In contrast to DPSH, ADSH, and DAPH, although RADH obtains a slight enhancement on the MAP scores when the bit length is 8 and 12, it achieves larger improvement when the code length ranges from 16 to 48. Particularly, RADH reaches 80.13% and 80.38% when the code length is 36 and 48, respectively, while the best results gained by the three deep hashing approaches are only 76.20% and 76.05%, being far lower than that obtained by RADH.

Referring to MAP@Top500 and Precision@Top500 scores tabulated in Table IX, our method has more remarkable achievement. In contrast to LSH, SpH, ITQ, and DSH, there is more than 10% improvement on both evaluation protocols. Compared with the three deep hashing methods, RADH gains also about 2%–4% enhancement when the code length ranges from 8 to 48.

The PR curves on the MIRFLICKR-25K data set computed by LSH, SpH, ITQ, DSH, DPSH, ADSH, DAPH, and RADH are shown in Fig. 7. As we can see, although RADH has a similar result compared with ADSH when the code length is 8, it covers larger areas in other situations. Particularly, with the increase in the code length, our presented approach enlarges the gap of covered areas compared with the three deep learning based hashing methods. Furthermore, in Fig. 7, despite the fact that ADSH has a competitive performance on the PR curve, it is inferior to DPSH when the code length increases to 24, 36, and 48, indicating its instability. By contrast, RADH always obtains the competitive or best performance no matter how long the code length is, which demonstrates the effectiveness and robustness of our method.

As mentioned above, to accelerate the speed, RADH samples a part of training samples in each training epoch. To make a fair comparison, we remove this sampling operation in RADH and reconduct experiments when the code length is set to 16-bit. The results of the three metrics are (78.96, 76.59, 80.91), (64.18, 72.92, 73.12), (48.55, 62.27, 59.80), and (76.83, 85.09, 84.27) for the four data sets, respectively. Obviously, there is a slight improvement for ADSH if all the training samples are used in each epoch. However, compared with our proposed method RADH, ADSH is still inferior.

Totally, RADH achieves the best performances except one case in Table V. In fact, both the distributions of different data...
sets and the numbers of training samples can influence the performance. To demonstrate the superiority of the proposed method, it should achieve better performances on most of data sets. In other words, it is possible that the proposed method is inferior to other comparison methods in some specific cases. Particularly, in Table I, RADH obtains much higher results of the performance gap is quite small on the MAP score. When $\eta$ is located in the ranges of [0.01, 4], [0.01, 5], [0.01, 5] and [0.01, 5] for these four data sets, RADH can always achieve satisfactory performance.

The influences on the experimental results with different values of $\gamma$ are shown in Fig. 9. Note that the $\tau$ is set to 0.1 for the four data sets. The $\eta$ is set to 0.3 for the NUS-WIDE, IAPR TC-12 and MIRFLICK-25K data sets, while it is set to 1 for the CIFAR-10 data set. From this figure, we can observe that our presented approach is also insensitive to $\gamma$. When $\gamma$ is located in the range from 100 to 700, the maximum of the performance gap is quite small on the MAP score.

Fig. 10 plots the MAP, MAP@Top500, and Precision@Top500 scores when $\tau$ ranges from 0.0001 to 10. Note that in this experiment, $\gamma$ is set to 500 for the four data sets. The $\eta$ is also set to 1 for the first data set and 0.3 for the last three data sets. As we can see, with the increase of $\tau$, there is about 2%–3% enhancement on the MAP scores for the four data sets, which indicates the effectiveness of our proposed triplet loss. Additionally, $\tau$ also has a wide choice from 0.01 to 1, demonstrating its robustness.

Referring to the learning rate, we set it to $10^{-1}$, $10^{-2}$, $10^{-3}$, $10^{-4}$, and $10^{-5}$ for all the data sets, respectively, when the code length is 16-bit. Their corresponding results are shown in Table X. As we can see, the learning rate with a large value would result in divergence or fluctuation, while the learning rate with a tiny value would make the network converge too slow, which may also influence the performance. A typical example is the experiment on the CIFAR-10, in which too large or too small learning rates have the inferior influence on the performance. Thus, a suitable learning rate is $10^{-3}$.

Table XI lists the results obtained by RADH when the batch size changes from 16 to 128. Note that the code length is set to 16-bit. It is easy to observe that our proposed method is robust on the batch size, which is similar to many deep learning methods [15], [16]. Thus, we empirically set it to 64 for all of the four data sets.
Fig. 8. MAP, MAP@Top500, and Precision@Top500 scores under the change of $\eta$. Results conducted on (a) CIFAR-10, (b) NUS-WIDE, (c) IAPR TC-12, and (d) MIRFLICK-25K.

Fig. 9. MAP, MAP@Top500, and Precision@Top500 scores under the change of $\gamma$. Results conducted on (a) CIFAR-10, (b) NUS-WIDE, (c) IAPR TC-12, and (d) MIRFLICK-25K.

Fig. 10. MAP, MAP@Top500, and Precision@Top500 scores under the change of $\tau$. Results conducted on (a) CIFAR-10, (b) NUS-WIDE, (c) IAPR TC-12, and (d) MIRFLICK-25K.

Referring to updating the variable $B$ in (21), in fact, there is an inner iteration when a column is updated while others are fixed. In the aforementioned experiments, we set this inner iteration to be 1. In fact, Huiskes and Lew [52] have proven that setting the iteration number to be 1 for the subproblem can also get similar solutions if the iteration for the whole problem is large enough. Here we have conducted additional experiments by setting this inner iteration number to be 10 and the results are tabulated in Table XII. Note the code length is set to 16-bit. It is easy to see that RADH obtains similar results compared with results in Tables II–IX, demonstrating the reasonability of the $B$ updating strategy.
In this article, an RADH method is proposed. Different from the most existing methods that achieve the matching between each pair of instances through a point-to-point way, we relax it to a point-to-angle way. Specifically, there is no length constraint on the learned real-valued features, while the asymmetric strategy encourages the discrete hashing variables and real-valued features to be located in the same Hamming space if they share the same semantic information. In addition, to further make a good ranking for the positive and negative pairs, a novel triplet loss is proposed, which is quite adaptive for the hashing learning. Experiments conducted on four real-world data sets demonstrate the superiority of our proposed approach.

V. Conclusion

In this article, an RADH method is proposed. Different from the most existing methods that achieve the matching between each pair of instances through a point-to-point way, we relax it to a point-to-angle way. Specifically, there is no length constraint on the learned real-valued features, while the asymmetric strategy encourages the discrete hashing variables and real-valued features to be located in the same Hamming space if they share the same semantic information. In addition, to further make a good ranking for the positive and negative pairs, a novel triplet loss is proposed, which is quite adaptive for the hashing learning. Experiments conducted on four real-world data sets demonstrate the superiority of our proposed approach.

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